B.A./B. Sc./B.Com./B.C.A/B.S.W. DEGREE EXAMINATION, APRIL 2009 SECOND SEMESTER

| COURSE | $:$ GENERAL ELECTIVE |
| :--- | :--- |
| PAPER | $:$ OPERATIONS RESEARCH |
| TIME | $: 2$ HOURS |

SECTION - A

## ANSWER ANY TEN QUESTIONS:

MAX. MARKS: 100

1. Define OR
2. State any two characteristics of OR.
3. What are the different methods of obtaining an initial feasible solution to a transportation problem?
4. Solve the following assignment problem to minimize total time

> Job

Time in hours

| Machines |  | J1 | J2 | J3 | J4 | J5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | M1 | 7 | 5 | 9 | 8 | 11 |
|  | M2 | 9 | 12 | 7 | 11 | 10 |
|  | M3 | 8 | 5 | 4 | 6 | 9 |
|  | M4 | 7 | 3 | 6 | 9 | 5 |
|  | M5 | 4 | 6 | 7 | 5 | 11 |

5. Define an unbalance assignment problem.
6. Seven jobs go first over machine I and then over machine II, processing time in hours are given as

| Job | A | B | C | D | E | F | G |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Machine I | 6 | 24 | 30 | 12 | 20 | 22 | 18 |
| Machine II | 16 | 20 | 20 | 12 | 24 | 2 | 6 |

Find the optimal sequence in which the jobs should be processed.
7. Define a strategy. What are the different types of strategy?
8. Find the saddle point of the following game:

Player B

Player A

|  | B1 |  | B2 |  |
| :---: | :---: | :---: | :---: | :---: |
| B3 | B4 |  |  |  |
| A11 | 20 | 15 | 12 | 35 |
| A2 | 25 | 14 | 8 | 10 |
| A3 | 40 | 2 | 10 | 5 |
| A4 | -5 | 4 | 11 | 0 |
|  |  |  |  |  |

9. State Dominance Principle.
10. Define (i) Event (ii) Critical Path
11. What are the different types of time estimates in PERT?
12. Explain the term resource smoothing in network.

## SECTION - B

## ANSWER ANY FOUR QUESTIONS:

$(4 \times 20=80)$
13. a) A manufacturer wants to ship 22 loads of his product as given below. The matrix gives the kilometres from sources of supply to the destination.

Destination

S!
S2
Source

> S3

Demand

| D1 | D2 | D3 | D4 | D5 |
| :---: | :---: | :---: | :---: | :---: |
| 5 | 8 | 6 | 6 | 3 |
| 4 | 7 | 7 | 6 | 5 |
| 8 | 4 | 6 | 6 | 4 |
| 4 | 4 | 5 | 4 | 8 |

Supply
8
5
9
Shipping cost is Rs.10/load/km. What shipping schedule should be used to minimize total transportations cost?
b) Give the mathematical formulation of an assignment problem.
14. a) Solve the following traveling salesman problem to minimize the total cost.

## To

Cost-lines ‘000

From

|  |  |  | A |  | B |
| :---: | :---: | :---: | :---: | :---: | :---: |
| C | D |  | E |  |  |
| A | $\infty$ | 2 | 5 | 7 | 1 |
| B | 6 | $\infty$ | 3 | 8 | 2 |
| C | 8 | 7 | $\infty$ | 4 | 7 |
|  | D | 12 | 4 | 6 | $\infty$ |
| E | 1 | 3 | 2 | 8 | $\infty$ |
|  |  |  |  |  |  |

b) Reduce the following two-person zero sum game to $2 \times 2$ game and obtain optimal strategies for each player and the value of the game.

Player B

Player A

|  | B1 |  | B2 | B3 |
| :---: | :---: | :---: | :---: | :---: |
| A1 4 |  |  |  |  |
|  | 3 | 2 | 4 | 0 |
| A2 | 3 | 4 | 2 | 4 |
| A3 | 4 | 2 | 4 | 0 |
| A4 | 0 | 4 | 0 | 8 |
|  |  |  |  |  |

15. A project has the following time schedule.

| Activity | Time (in months) | Activity | Time (in months) |
| :---: | :---: | :---: | :---: |
| $1-2$ | 2 | $3-7$ | 5 |
| $1-3$ | 2 | $4-6$ | 3 |
| $1-4$ | 1 | $5-8$ | 1 |
| $2-5$ | 4 | $6-9$ | 5 |
| $3-6$ | 8 | $7-8$ | 4 |
|  |  | $8-9$ | 3 |

(i) Draw the network
(ii) Find the earliest and latest times for each event
(iii) Determine the critical path and its duration
(iv) Determine the total and free float.
16. a) $X Y Z$ Company has five jobs $A, B, C, D, E$ to be done and five men $L, M, N, O, P$ to do these jobs. The number of hours each man would take to accomplish each job is given by the following table.

Men

Jobs

|  | L |  | M | N | O |
| :---: | :---: | :---: | :---: | :---: | :---: |
| A | P |  |  |  |  |
|  | 4 | 6 | 11 | 16 | 9 |
|  | 5 | 8 | 16 | 19 | 9 |
| C | 9 | 13 | 21 | 21 | 13 |
| D | 6 | 6 | 9 | 11 | 7 |
| E | 11 | 11 | 16 | 26 | 11 |
|  |  |  |  |  |  |

Find the optimal schedule with time for the assignment problem to minimize total cost.
b) Discuss the differences between CPM and PERT.
17. a) Find the sequence, for the following eight jobs, that will minimize the total elapsed time for the completion of all the jobs. Each job is processed in the same order CAB . Entries give the time in hours on machines.
Jobs Times
on
Machines

|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | 4 | 6 | 7 | 4 | 5 | 3 | 6 | 2 |
| B | 8 | 10 | 7 | 8 | 11 | 8 | 9 | 13 |
| C | 5 | 6 | 2 | 3 | 4 | 9 | 15 | 11 |

b) Solve the game given in the table below by graphic method:

Player B

Player A

|  |  |  | B1 | B2 |
| :---: | :---: | :---: | :---: | :---: |
| B3 | B4 |  |  |  |
| A1 | 19 | 6 | 7 | 5 |
| A2 | 7 | 3 | 14 | 6 |
| A3 | 12 | 8 | 18 | 4 |
| A4 | 8 | 7 | 13 | -1 |
|  |  |  |  |  |

18. A Project consists of the following activities and different time estimates

| Activity | $\mathrm{t}_{0}$ | $\mathrm{t}_{\mathrm{p}}$ | $\mathrm{t}_{\mathrm{m}}$ |
| :---: | :---: | :---: | :---: |
| $1-2$ | 3 | 15 | 6 |
| $1-3$ | 2 | 14 | 5 |
| $1-4$ | 6 | 30 | 12 |
| $2-5$ | 2 | 8 | 5 |
| $2-6$ | 5 | 17 | 11 |
| $3-6$ | 3 | 15 | 6 |
| $4-7$ | 3 | 27 | 9 |
| $5-7$ | 1 | 7 | 4 |
| $6-7$ | 2 | 8 | 5 |

(i) Draw the network
(ii) Determine the expected task times and their variances.
(iii) Find the earliest and latest expected times to reach node.
(iv) Find the critical path
(v) What is the probability that the project will be completed by 27 days

