STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI – 86 (For candidates admitted during the academic year 2004–05 & thereafter)

SUBJECT CODE: EC/PE/MM24

M. A. DEGREE EXAMINATION, APRIL 2007 BRANCH III – ECONOMICS SECOND SEMESTER

COURSE : ELECTIVES

PAPER : MATHEMATICAL METHODS - II

TIME : 3 HOURS MAX. MARKS : 100

SECTION - A

ANSWER ANY FIVE QUESTIONS.

 $(5 \times 8 = 40)$

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- 1. Explain the properties of Determinants.
- 2. (a) Define Diagonal, Identity and Idempotent matrices.
 - (b) Find the rank of the matrix

$$\mathbf{A} = \begin{bmatrix} 1 & 3 & 4 & -2 \\ 2 & 6 & 8 & -4 \\ 3 & 0 & 3 & 3 \end{bmatrix}$$

- 3. Explain the Technological coefficient matrix.
- 4. If $\beta = 4$ and C = 0.8, Find the time path of Y in Samuelson's trade cycle model.
- 5. Solve the following LPP with the help of Graphical Method

Maximise
$$f = 2x + 5y$$

Subject to $x + 4y \le 24$
 $3x + y \le 21$
 $x + y \le 9$
 $x \text{ and } y \ge 0$

- 6. Briefly explain the basic elements of Game Theory.
- 7. (a) Bring all the rules of transformation to obtain the Dual
 - (b) Obtain dual of the following LPP

Maximise
$$F = 2x_1 + 3x_2$$

Subject to $x_1 + 3x_2 \le 12$
 $2x_1 + x_2 \ge 6$
 $x_1 + 5x_2 = 10$
 $x_1, x_2 \ge 0$

SECTION - B

ANSWER ANY THREE QUESTIONS

 $(3 \times 20 = 60)$

8. (a) Find the inverse of the matrix

$$\mathbf{A} = \begin{bmatrix} 1 & 4 & 3 \\ 4 & 2 & 1 \\ 3 & 2 & 2 \end{bmatrix}$$

(b) Solve the following equation by Cramer's Rule

$$x - 2y + 3z = 1$$

 $3x - y + 4z = 3$
 $2x + y - 2z = -1$

9. Given
$$A = \begin{bmatrix} 0.1 & 0.3 & 0.1 \\ 0 & 0.2 & 0.2 \\ 0 & 0 & 0.3 \end{bmatrix}$$

and final demands are F_1 F_2 & F_3 . Find the output levels consistent with the model. What will be output levels if $F_1 = 20$, $F_2 = 0$ & $F_3 = 100$

- 10. (a) Solve $Y_t = 2y_{t-1} + t$
 - (b) Explain the cobweb model by using difference equation
- 11. Maxmise $z = x_1 + 4x_2 + 5x_3$

Subject to the constraints

$$3x_1 + 3x_3 \le 22$$

 $x_1 + 2x_2 + 3x_3 \le 14$
 $3x_1 + 2x_2 \le 14$
 $x_1 \ge 0, x_2 \ge 0, x_3 \ge 0$

12. (a) Explain Two Person Zero sum game

(b) Solve the following game
$$\begin{bmatrix} 3 & -5 & -4 \\ -2 & 1 & 2 \\ 1 & 1 & 2 \end{bmatrix}$$
