STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI 600 086 (For candidates admitted during the academic year 2015 – 16)

SUBJECT CODE : 15MT/PC/FD34

M. Sc. DEGREE EXAMINATION, NOVEMBER 2016 BRANCH I - MATHEMATICS THIRD SEMESTER

COURSE	: CORE	
PAPER	: FLUID DYNAMICS	
TIME	: 3 HOURS	MAX. MARKS: 100

SECTION – A

ANSWER ALL THE QUESTIONS:

 $(5 \times 2 = 10)$

- 1. Define path lines.
- 2. What are the conditions satisfied at the boundary of two inviscid immiscible fluids?
- 3. Define a dipole.
- 4. Define line source and line sink.
- 5. Define stress matrix.

SECTION – B

ANSWER ANY FIVE QUESTIONS:

 $(5 \times 6 = 30)$

- 6. Discuss the acceleration of a fluid.
- 7. Show that at all points in the field of flow the equipotential are cut orthogonally by the stream lines.
- 8. Derive Bernoulli's equation.
- 9. a. Show that in two dimensional flow the vorticity vector is perpendicular to the plane of flow.

b. Discuss the flow due a uniform line doublet at 0 of strength μ per unit length, its axis

being along \overline{OX} .

- 10. Discuss the uniform flow past a fixed infinite circular cylinder.
- 11. Obtain the image of a line source in a circular cylinder.
- 12. Discuss the stress analysis in fluid motion.

SECTION – C

ANSWER ANY THREE QUESTIONS:

 $(3 \times 20 = 60)$

- 13. a. Derive equation of continuity.
 - b. For a fluid moving in a fine tube of variable section A, prove from first principles that the equation of continuity is A where ν is the speed at a point P of the fluid and s the length of the tube up to P. What does this become for steady incompressible flow?
- 14. a. Derive Euler's equation of motion.

b. Discuss the steady motion under conservative body forces.

- 15. Define Stoke's stream function $\psi(r, \theta)$ for the symmetric flow of an incompressible fluid. Also determine the stream function corresponding to a uniform stream *U*.
- 16. a.State and prove Milne Thompson Circle theorem.
 - b. Determine the irrotational motion of a incompressible liquid for which the complex potential $\omega = ik \log z$.
- 17. Discuss steady motion between parallel planes.
