STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI 600 086 (For candidates admitted during the academic year 2015 – 16& thereafter)

SUBJECT CODE: 15MT/PC/DE14

M. Sc. DEGREE EXAMINATION, NOVEMBER 2016 BRANCH I - MATHEMATICS FIRST SEMESTER

COURSE : CORE

PAPER : DIFFERENTIAL EQUATIONS

TIME : 3 HOURS MAX. MARKS : 100

SECTION - A (5 X 2 = 10)

ANSWER ALL QUESTIONS

1. Define Wronskian of two functions.

- 2. State Lipschitz condition.
- 3. Find a complete integral of $q = 3p^2$.
- 4. Define Boundary value problems.
- 5. Define Dirichlet problem.

SECTION - B (5 X 6 = 30)

ANSWER ANY FIVE QUESTIONS

- 6. If P_n is a legendre polynomial then prove that $\int_{-1}^1 P_n^2(t) dt = \frac{2}{2n+1}$.
- 7. State and prove Abel's formula.
- 8. Find the complete integral of zpq=p+q by charpits method.
- 9. Reduce $\left(\frac{\partial^2 z}{\partial x^2}\right) = x^2 \left(\frac{\partial^2 z}{\partial y^2}\right)$ to canonical form.
- 10. Derive one dimensional wave equation.
- 11. An insulated rod of length l has its ends A and B at 0^{0} c and 100^{0} c respectively until steady state conditions prevail . If B is suddenly reduced to 0^{0} c and maintained at 0^{0} c find the temperature at a distance x from A at time t'.
- 12. Find the steady state temperature distribution in a thin rectangular plate bounded by the lines x = 0, x = a, y = 0, y = b. The edges x = 0, x = a, y = 0 are kept at temperature zero while the edge y = b is kept at 100^{0} C.

 $(3 \times 20 = 60)$

ANSWER ANY THREE QUESTIONS

- 13. Solve the Bessel equation $t^2x'' + tx' + (t^2 p^2)x = 0$ of order p.
- 14. State and prove picard's theorem.
- 15. (a) Find a complete integral of $z^2 = pqxy$ by using charpits method.
- (b) Reduce the equation $(n-1)^2 \left(\frac{\partial^2 z}{\partial x^2}\right) y^{2n} \left(\frac{\partial^2 z}{\partial y^2}\right) = n y^{2n-1} \left(\frac{\partial z}{\partial y}\right)$ to canonical form.
- 16. (a)Obtain the general solution of heat flow equation $k\left(\frac{\partial^2 u}{\partial x^2}\right) = \frac{\partial u}{\partial t}$ by the method of separation of variables.
 - (b)Discuss D' Alembert's solution of wave equation.
- 17. Solve two dimensional Laplace equation in plane polar co-ordinates (r, θ) .

