### STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI 600 086 (For candidates admitted during the academic year 2015 – 16)

## SUBJECT CODE: 15MT/AC/BM35

## B. Com. DEGREE EXAMINATION, NOVEMBER 2016 CORPORATE SECRETARYSHIP THIRD SEMESTER

COURSE	:	ALLIED – CORE
PAPER	:	<b>BUSINESS MATHEMATICS</b>
TIME	:	3 HOURS

MAX. MARKS: 100

(10 X 2 = 20)

#### SECTION – A ANSWER ALL THE QUESTIONS

1. Define a scalar matrix with an example.

2. If A= (1 2 3 4) and B = 
$$\begin{pmatrix} 1 \\ 2 \\ 3 \\ 4 \end{pmatrix}$$
 find AB and BA.

- 3. Find the value of k if 3+2i is a root of the equation  $x^2 6x + k = 0$
- 4. If  $\alpha, \beta, \gamma$  are the roots of  $x^3 + px^2 + qx + r = 0$  find the value of  $\alpha^2 + \beta^2 + \gamma^2$
- 5. Show that the root of  $x^3 6x 13 = 0$  lies between 3 and 4.
- 6. Solve the linear system  $x_1 4x_2 = -2$ ;  $3x_1 + x_2 = 7$  by Gauss-Jordan method.

7. If 
$$y = \frac{x-1}{x+1}$$
 find  $\frac{dy}{dx}$ 

8. If 
$$y = (3x^2 + 4x - 5)^3$$
 find  $\frac{dy}{dx}$ 

- 9. Evaluate  $\frac{4x^3}{x^4+1} dx$ .
- 10. Evaluate  $xe^{x}dx$ .

#### SECTION – B ANSWER ANY FIVE QUESTIONS

(5 X 8 = 40)

- 11. Verify Cayley Hamilton theorem for  $\begin{pmatrix} 1 & 2 & 3 \\ 0 & -1 & 2 \\ 1 & 0 & 2 \end{pmatrix}$  and hence find its inverse.
- 12. Solve  $x^4 5x^3 + 4x^2 + 8x 8 = 0$ , given that  $1 + \overline{5}$  is a root.
- 13. Solve  $2x^3 3x^2 11x + 6 = 0$  given its roots are in Arithmetic Progression.
- 14. Evaluate  $\overline{12}$  to four decimal places by Newton Raphson method.
- 15. Solve the following system of equations by Gaussian elimination method.

 $x_1 - x_2 + x_3 = 1$ ;  $-3x_1 + 2x_2 - 3x_3 = -6$ ;  $2x_1 - 5x_2 + 4x_3 = 5$ 

16. The total cost function for the production of x units of an item is given by  $10-4x^3+3x^4$ . Find (i) The average cost (ii) The marginal cost (iii) The marginal average cost.

17. Evaluate 
$$\frac{x}{(x-1)(2x+1)} dx$$
.

# $SECTION - C \qquad (2 X 20 = 40)$ ANSWER ANY TWO QUESTIONS

- 18. (a) Find the Eigen values and Eigen vectors of  $\begin{pmatrix} 1 & 1 & 3 \\ 1 & 5 & 1 \\ 3 & 1 & 1 \end{pmatrix}$ .
  - (b) Solve  $2x^5 + 7x^4 + 9x^3 + 9x^2 + 7x + 2 = 0$  (10+10 marks)

19. Solve the system of equations using Gauss-Seidel method:

8x - y + z - 18 = 0; 2x + 5y - 2z - 3 = 0; x + y - 3z + 6 = 0

20. (a) Find the maximum and minimum values of  $2x^3 - 3x^2 - 36x + 10$ 

(b) The marginal cost of production of a firm is given by C' x = 5 + 0.13x. The marginal revenue is given by R'(x)=18. The fixed cost is Rs.120. Find the profit function. (10+10 marks)