SUBJECT CODE : 15MT/AC/BM35

## B. Com. DEGREE EXAMINATION, NOVEMBER 2016 <br> CORPORATE SECRETARYSHIP THIRD SEMESTER

COURSE : ALLIED - CORE
PAPER : BUSINESS MATHEMATICS
TIME : 3 HOURS MAX. MARKS : 100

## SECTION - A <br> ANSWER ALL THE QUESTIONS

( $10 \times 2=20$ )

1. Define a scalar matrix with an example.
2. If $\mathrm{A}=\left(\begin{array}{lll}1 & 2 & 3\end{array} 4\right)$ and $\mathrm{B}=\left(\begin{array}{l}1 \\ 2 \\ 3 \\ 4\end{array}\right)$ find AB and BA .
3. Find the value of $k$ if $3+2 i$ is a root of the equation $x^{2}-6 x+k=0$
4. If $\alpha, \beta, \gamma$ are the roots of $\mathrm{x}^{3}+\mathrm{px}^{2}+\mathrm{qx}+\mathrm{r}=0$ find the value of $\alpha^{2}+\beta^{2}+\gamma^{2}$
5. Show that the root of $x^{3}-6 x-13=0$ lies between 3 and 4 .
6. Solve the linear system $x_{1}-4 x_{2}=-2 ; 3 x_{1}+x_{2}=7$ by Gauss-Jordan method.
7. If $y=\frac{x-1}{x+1}$ find $\frac{d y}{d x}$.
8. If $y=\left(3 x^{2}+4 x-5\right)^{3}$ find $\frac{d y}{d x}$.
9. Evaluate $\frac{4 x^{3}}{x^{4}+1} d x$.
10. Evaluate $x e^{x} d x$.

> SECTION - B
$(5 \times 8=40)$
ANSWER ANY FIVE QUESTIONS
11. Verify Cayley Hamilton theorem for $\left(\begin{array}{ccc}1 & 2 & 3 \\ 0 & -1 & 2 \\ 1 & 0 & 2\end{array}\right)$ and hence find its inverse.
12. Solve $x^{4}-5 x^{3}+4 x^{2}+8 x-8=0$, given that $1+\overline{5}$ is a root.
13. Solve $2 x^{3}-3 x^{2}-11 x+6=0$ given its roots are in Arithmetic Progression.
14. Evaluate $\overline{12}$ to four decimal places by Newton - Raphson method.
15. Solve the following system of equations by Gaussian elimination method.

$$
x_{1}-x_{2}+x_{3}=1 ;-3 x_{1}+2 x_{2}-3 x_{3}=-6 ; 2 x_{1}-5 x_{2}+4 x_{3}=5
$$

16. The total cost function for the production of $x$ units of an item is given by $10-4 x^{3}+3 x^{4}$. Find (i) The average cost (ii) The marginal cost (iii) The marginal average cost.
17. Evaluate $\frac{x}{(x-1)(2 x+1)} d x$.

## SECTION - C <br> ANSWER ANY TWO QUESTIONS

$(2 \times 20=40)$
18. (a) Find the Eigen values and Eigen vectors of $\left(\begin{array}{lll}1 & 1 & 3 \\ 1 & 5 & 1 \\ 3 & 1 & 1\end{array}\right)$.
(b) Solve $2 x^{5}+7 x^{4}+9 x^{3}+9 x^{2}+7 x+2=0$
(10+10 marks)
19. Solve the system of equations using Gauss-Seidel method:

$$
8 x-y+z-18=0 ; \quad 2 x+5 y-2 z-3=0 ; \quad x+y-3 z+6=0
$$

20. (a) Find the maximum and minimum values of $2 x^{3}-3 x^{2}-36 x+10$
(b) The marginal cost of production of a firm is given by $C^{\prime} x=5+0.13 x$. The marginal revenue is given by $\mathrm{R}^{\prime}(\mathrm{x})=18$. The fixed cost is Rs. 120 .

Find the profit function.
(10+10 marks)

