STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI 600 086 (For candidates admitted from the academic year 2015-16)

SUBJECT CODE: 15MT/PE/ME14

M. Sc. DEGREE EXAMINATION, APRIL 2016 BRANCH I – MATHEMATICS SECOND SEMESTER

COURSE : ELECTIVE PAPER : MECHANICS

TIME : 3 HOURS MAX. MARKS: 100

SECTION - A

Answer allthe questions:

 $5 \times 2 = 10$

- 1. Write down conservation theorem for the Linear Momentum of a particle.
- 2. Define energy function h.
- 3. Explain orthogonality condition for a linear transformation.
- 4. Define free energy and write down the differential equation for its property.
- 5. Write the transformation of configuration space and phase space.

SECTION - B

Answer any fivequestions:

 $5 \times 6 = 30$

- 6. Give an example for non-holonomic constraint.
- 7. Discuss geodesics problem.
- 8. Explain general conservation theorem.
- 9. Obtain Euler's equations of motion for a rigid body with one point fixed.
- 10. Obtain Hamilton's canonical equations of motion.
- 11. Discuss the Routh's procedure of the particle moving in a plane under the influence of a central force derived from a potential function V(r).
- 12. Obtain the new Hamiltonian function for the first two generating functions.

SECTION - C

Answer any three questions:

 $3 \times 20 = 60$

- 13. a)Obtain Lagrange's equation of motion for a holonomic system.
 - b) Obtain the equation of motion of the particle using plane polar coordinates. (10+10)
- 14. a) Discuss the brachistochrone problem.
 - b) Obtain Euler-Lagrange differential equations.(10+10)

- 15. a) Obtain the expression for the Kinetic energy of a rigid body with one point interms of the inertia coefficients.
 - b) State and prove parallel Axes theorem.

(10+10)

- 16. Obtain Jacobi's form of principle of least action.
- 17. Explain in detail the symplectic approach to canonical transformation.

