## M.A. DEGREE EXAMINATION NOVEMBER 2009 <br> BRANCH III - ECONOMICS <br> FIRST SEMESTER

| COURSE | : ELECTIVE |
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| PAPER | : MATHEMATICAL METHODS - I |
| TIME | $: 3$ HOURS |

MAX.MARKS : 100

## SECTION - A

## ANSWER ANY FIVE QUESTIONS. EACH ANSWER NOT TO EXCEED 300

WORDS:
( $5 \times 8=40$ )

1. a) What is a continuous function?
b) Select the graph of the limit of a function: $\lim _{x \rightarrow 7} f(x)=4$
2. Find the successive derivative of the function:

$$
f(x)=2 x^{4}+5 x^{3}+3 x^{2}
$$

and also interpret the second - order derivative as measure.
3. Find the first order derivative of the following functions:
a) $y=\left(\frac{x+1}{x-1}\right)^{2}$
b) $y=\log \left(4 x^{5}-3 x^{2}+6 x\right)^{3}$
4. Given the demand function $P=30-2 Q$
a) Find the marginal Revenue at $Q=4$
b) Find the marginal cost at $Q=2$ if $T C=Q^{2}+7 Q+23$
5. Distinguish between
i) increasing and decreasing functions
ii) Concavity and convexity functions with suitable diagrams
6. Prove the elasticity of substitution, $\sigma$ of Cobb - Douglas production function is unitary.
7. a) Marginal cost is given by $\mathrm{MC}=25+30 Q-9 Q^{2}$. Fixed cost is 55 . Find the
i) total cost, ii) average cost and iii) variable cost functions.
b) Given the demand function $P=42-5 Q-Q^{2}$. Assuming equilibrium price is 6 , evaluate the consumer's surplus.

## SECTION - B

## ANSWER ANY THREE QUESTIONS: EACH ANSWER NOT TO EXCEED 1200 WORDS: $\quad(3 \times 20=60)$

8. For the following function: $y=x^{3}-18 x^{2}+96 x-80$

Find
i. The critical values
ii. Test for concavity to determine relative maxima or minima
iii. Check for inflection points
iv. Evaluate the function at the critical values and inflection points
9. Explain the properties of Cobb- Douglas Production functions
10. Find with two distinct demand functions
$Q_{1}=24-0.2 P_{1}$
$Q_{2}=10-0.05 P_{2}$

Where $T C=35+40 Q$, what price will be firm charge (a) with discrimination b) without discrimination
11. Optimize the function $z=4 x^{2}+3 x y+6 y^{2}$ subject to the constraint $x+y=56$
12. Explain the dynamics of growth in the economy with suitable example.

