SUBJECT CODE: EC/PE/MM13

M.A. DEGREE EXAMINATION NOVEMBER 2009 BRANCH III – ECONOMICS FIRST SEMESTER

COURSE	: ELECTIVE
PAPER	: MATHEMATICAL METHODS - I
TIME	: 3 HOURS

MAX.MARKS: 100

SECTION – A

ANSWER ANY FIVE QUESTIONS. EACH ANSWER NOT TO EXCEED 300 WORDS: (5 X 8 = 40)

- a) What is a continuous function ?
 b) Select the graph of the limit of a function: lim f(x) = 4
- 2. Find the successive derivative of the function: $f(x) = 2x^4 + 5x^3 + 3x^2$

and also interpret the second – order derivative as measure.

3. Find the first order derivative of the following functions:

a)
$$y = \left(\frac{x+1}{x-1}\right)^2$$

b)
$$y = \log(4x^5 - 3x^2 + 6x)^3$$

- 4. Given the demand function P = 30 2Q
 - a) Find the marginal Revenue at Q = 4
 - b) Find the marginal cost at Q = 2 if $TC = Q^2 + 7Q + 23$
- 5. Distinguish between
 - i) increasing and decreasing functions
 - ii) Concavity and convexity functions with suitable diagrams
- 6. Prove the elasticity of substitution, σ of Cobb Douglas production function is unitary.
- 7. a) Marginal cost is given by $MC = 25 + 30Q 9Q^2$. Fixed cost is 55. Find the i) total cost, ii) average cost and iii) variable cost functions.

b) Given the demand function $P = 42 - 5Q - Q^2$. Assuming equilibrium price is 6, evaluate the consumer's surplus.

SECTION – B

ANSWER ANY THREE QUESTIONS: EACH ANSWER NOT TO EXCEED 1200 WORDS: (3 X 20 = 60)

- 8. For the following function: $y = x^3 18x^2 + 96x 80$ Find
 - i. The critical values
 - ii. Test for concavity to determine relative maxima or minima
 - iii. Check for inflection points
 - iv. Evaluate the function at the critical values and inflection points
- 9. Explain the properties of Cobb- Douglas Production functions
- 10. Find with two distinct demand functions $Q_1 = 24 - 0.2P_1$ $Q_2 = 10 - 0.05P_2$

Where TC = 35 + 40Q, what price will be firm charge (a) with discrimination b) without discrimination

- 11. Optimize the function $z = 4x^2 + 3xy + 6y^2$ subject to the constraint x + y = 56
- 12. Explain the dynamics of growth in the economy with suitable example.
