

M. Sc. DEGREE EXAMINATION, APRIL 2015
BRANCH I – MATHEMATICS
FOURTH SEMESTER

COURSE : ELECTIVE
PAPER : MATHEMATICAL MODELING
TIME : 3 HOURS

MAX. MARKS: 100

SECTION –A

Answer all the questions:

5×2=10

1. Explain the principle of superposition.
2. Describe the lumped element model.
3. Draw the generic schematic of the variation of traffic velocity with density.
4. Explain the geometry of a planar pendulum.
5. Show that $\frac{1}{\lambda_H} \left(\ln \frac{H}{H_e} - \frac{H}{H_e} \right) + \frac{1}{\lambda_P} \left(\ln \frac{P}{P_e} - \frac{P}{P_e} \right) = \text{Constant}$, using parasite-host equation.

SECTION –B

Answer any five questions:

5×6=30

6. Explain dimensional homogeneity.
7. Explain Conservation and Balance principles.
8. In hovering, show that the power needed is proportional to $L^{7/2}$ and available power is proportional to L^2 .
9. Explain Conservation of Cars.
10. Consider a flow-density relationship of the form $q(\rho) = \rho(\alpha - \beta\rho)$. The best fit of this relationship to some real traffic data occurred when $\alpha = 91.33 \text{ km/hr}$ and $\beta = 1.4 \text{ km}^2 / \text{car.hr}$
 - (a) What is the maximum density?
 - (b) What is the maximum speed?
 - (c) What is the capacity of the road?

11. Discuss the dissipation of energy while the pendulum is moving and obtain

$$\frac{dE(t)}{dt} = -cI^2 \left(\frac{d\theta(t)}{dt} \right)^2 \text{ and hence show that } E(t) = E_0 e^{\left(-\frac{c}{m}\right)t}.$$

12. Derive $\frac{\tilde{T}_0}{T_0} \cong 1 + \frac{\theta_0^2}{16}$ for the nonlinear model of the freely-vibrating pendulum-III.

SECTION –C

Answer any three questions:

3×20=60

13. State and explain the Buckingham Pi theorem. Apply it to the Peanut butter mixer experiments and the classical pendulum experiment.
14. Describe the Scaling and Data acquisition in the cases:
- (i) rotational inertia of a wheel and
 - (ii) the diagnosis of a malfunctioning electronic device.
15. Discuss, in detail, an elementary Linear – Car following model.
16. Model the free vibration of pendulum with two masses m_1 and m_2 ; obtain its differential equation.
Discuss its solution in the cases : $m_2 < m_1$, $m_2 \ll m_1$, $m_2 > m_1$, $m_2 \gg m_1$ and $m_2 = m_1$
17. Obtain the Lotka-Volterra equations. Also, discuss the oscillatory solution for the Linearized Model.

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