

STELLA MARIS COLLEGE (AUTONOMOUS), CHENNAI – 600 086

M.Sc. DEGREE : BRANCH I – MATHEMATICS

**SYLLABUS**

(Effective from the academic year 2015-2016)

**NUMBER THEORY AND CRYPTOGRAPHY**

**CODE : 15MT/PE/NC14**

**CREDITS : 4**

**L T P : 4 0 0**

**TOTAL TEACHING HOURS : 52**

**OBJECTIVES OF THE COURSE**

- To provide an introductory course in Number theory
- To introduce the fast growing and relevant topic of cryptography as an application of Number theory

<b>Unit 1</b>	<b>Elementary Number Theory</b> 1.1 Time Estimates for doing Arithmetic 1.2 Divisibility and the Euclidean Algorithm	<b>(8 hrs.)</b>
<b>Unit 2</b>	<b>Elementary Number Theory (contd.)</b> 2.1 Congruences 2.2 Some Applications to Factoring	<b>(8 hrs.)</b>
<b>Unit 3</b>	<b>Finite Fields and Quadratic Residues</b> 3.1 Finite Fields 3.2 Quadratic Residues and Reciprocity	<b>(12 hrs.)</b>
<b>Unit 4</b>	<b>Cryptography</b> 4.1 Some Simple Cryptosystems 4.2 Enciphering Matrices	<b>(12 hrs.)</b>
<b>Unit 5</b>	<b>Public Key</b> 5.1 Public Key Cryptography 5.2 RSA 5.3 Pseudoprimes 5.4 The Rho Method	<b>(12 hrs.)</b>

## TEXT BOOK

Koblitz, Neal, *A Course in Number Theory and Cryptography*, second edition, New York: Springer – Verlag, 2002.

Chapter 1: Sec. 1 – 4

Chapter 2: Sec. 1, 2

Chapter 3: Sec. 1, 2

Chapter 4: Sec. 1, 2

Chapter 5: Sec. 1, 2

## BOOKS FOR REFERENCE

Christof Paar, Srivastava,R.J, *Understanding Cryptography*, New York: Springer, 2010.

Delfs Hans , Srivastava,R.J, *Introduction to cryptography, Principles and applications*, New York: Springer, 2002.

Ireland K., and Michael Rosen, *A Classical Introduction to Modern Number Theory*, second edition, New York: Springer Verlag, 2004.

## JOURNALS

Journal of Number Theory

INTEGERS: Electronic Journal of Combinatorial Number Theory

Turkish Journal of Analysis and Number Theory

International Journal of Number Theory

## WEB RESOURCES

<http://www.math.utk.edu/~finotti/papers/grad.pdf>

<http://www.cse.iitd.ernet.in/~bagchi/courses/discrete-book/ch2.pdf>

[http://almuhammadi.com/sultan/crypto\\_books/Koblitz.2ndEd.pdf](http://almuhammadi.com/sultan/crypto_books/Koblitz.2ndEd.pdf)

## PATTERN OF EVALUATION

### Continuous Assessment:

**Total Marks: 50**

**Duration: 90 Mins.**

Section A:  $2 \times 2 = 4$  (Two questions to be set)

Section B:  $2 \times 6 = 12$  (Three questions to be set)

Section C:  $2 \times 17 = 34$  (Three questions to be set)

### Third Component :

List of evaluation modes:

Seminars

Quiz

Open Book Tests

Group Discussion

Assignments

Project

Theorem Writing Technique

Problem Solving

**End Semester Examination:**

**Total Marks: 100**

**Duration: 3 Hours**

Section A :  $5 \times 2 = 10$  (Five questions to be set, selecting one question per unit)

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Section C :  $3 \times 20 = 60$  (Five questions to be set without omitting any unit).

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**M.Sc. DEGREE : BRANCH I - MATHEMATICS**

**SYLLABUS**  
**(Effective from the academic year 2015 – 2016)**

**ANALYSIS OF ALGORITHMS**

**CODE : 15MT/PE/AA14**

**CREDIT : 4**

**L T P : 4 0 0**

**TOTAL TEACHING HOURS : 52**

**OBJECTIVES OF THE COURSE**

- To introduce different methods to solve problems in an abstract setup
- To analyse algorithms to choose the better algorithm

**Unit 1 (8 hrs.)**

**Analysis of Algorithm**

- 1.1 Input Classes
- 1.2 Space Complexity
- 1.3 Cases to Consider
- 1.4 Rates of Growth
- 1.5 Divide and Conquer Algorithms
- 1.6 Recurrence Relations

**Unit 2 (10 hrs.)**

**Searching and Selection Algorithms**

- 2.1 Binary Search - Case Analysis
- 2.2 Selection

**Unit 3 (11 hrs.)**

**Sorting Algorithms**

- 3.1 Insertion Sort - Case Analysis
- 3.2 Heap sort - Case Analysis
- 3.3 Quick sort - Case Analysis

**Unit 4 (13 hrs.)**

**Matching Algorithm**

- 4.1 String Matching
  - 4.2 Finite Automata
  - 4.3 Knuth-Morris-Pratt Algorithm
- Graph Algorithms**
- 4.4 Data Structures for Graphs
  - 4.5 Depth First and Breadth First Traversal Algorithms
  - 4.6 Minimum Spanning Tree Algorithms

- 4.7 The Dijkstra-Prim Algorithm
- 4.8 The Kruskal Algorithm

**Unit 5**

**(10 hrs.)**

**Nondeterministic Algorithms**

- 5.1 NP-Complete Problems
- 5.2 Conditions for NP
- 5.3 Job Scheduling – Graph Coloring

**TEXT BOOK**

McConnell, Jefferey J. *Analysis of Algorithms: An Active Learning Approach*, New Delhi: Narosa Publishing House, 2002.

Chapter 1	Sections 1.1, 1.1.1, 1.1.2, 1.2, 1.2.1, 1.4, 1.4.1, 1.5, 1.5.1, 1.5.2, 1.6
Chapter 2	Sections 2.2, 2.2.1, 2.2.2, 2.2.3, 2.3
Chapter 3	Sections 3.1, 3.1.1, 3.1.2, 3.5, 3.5.1, 3.5.2, 3.7, 3.7.1, 3.7.2
Chapter 5	Sections 5.1, 5.1.1, 5.1.2
Chapter 6	Sections 6.2, 6.2.1, 6.2.2, 6.3, 6.3.1, 6.3.2, 6.3.3, 6.4, 6.4.1, 6.4.2
Chapter 8	Sections 8.1 – 8.4

**BOOKS FOR REFERENCE**

Goodman and Hedetniemi. *Introduction to the Design and Analysis of Algorithms*. New Delhi: McGraw-Hill International Editions, 1997.

Horowitz Ellis, Sahni Sartaj and Rajasekaran Sanguthevar. *Fundamentals of Computer Algorithms*. 2<sup>nd</sup> ed. New Delhi: Galgotia Publciation Pvt. Ltd., 2007.

Loudon, Kyle. *Mastering Algorithms with C*. Mumbai: Shroff Publishers & Distributors Pvt. Ltd., 1999.

Gajavelli S.S., Bhishma Rao, *Discrete Structures and Graph Theory*. Chennai: Scitech Publications Pvt. Ltd., 2003.

**JOURNALS**

Journal of Algorithms & Computational Technology

Journal of Mathematical Modelling and Algorithms in Operations Research

**WEB RESOURCES**

Sedgewick Robert, Flajolet Phillippe, *An Introduction to the Analysis of Algorithms*, Pearson Education, Inc, 2013 (e-book)

[www.personal.kent.edu/~rmuhamma/Algorithms/algorithm.html](http://www.personal.kent.edu/~rmuhamma/Algorithms/algorithm.html)

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**M.Sc. DEGREE : BRANCH I – MATHEMATICS**

**SYLLABUS**  
**(Effective from the academic year 2015 – 2016)**

**SOFT SKILLS**

**CODE : 15MT/PK/SS22**

**CREDITS : 2**

**L T P : 2 0 0**

**TOTAL TEACHING HOURS : 26**

**OBJECTIVES OF THE COURSE**

- To empower and create opportunities for self development
- To instill confidence and face challenges

**Unit 1 (6 hrs)**

**Behavioural Traits**

- 1.1 Self Awareness
- 1.2 Communication Skills – Verbal and Non Verbal
- 1.3 Leadership Qualities
- 1.4 Etiquette and mannerisms
- 1.5 Experiential Learning – Based on activities

**Unit 2 (5 hrs)**

**Team Work**

- 2.1 Interpersonal Skills
- 2.2 People Management
- 2.3 Creative Thinking
- 2.4 Critical Thinking
- 2.5 Experiential Learning – Based on activities

**Unit 3 (5 hrs)**

**Time Management**

- 3.1 Importance of time management
- 3.2 Planning and Prioritizing
- 3.3 Organizing skills
- 3.4 Action Plan
- 3.5 Experiential Learning – Based on activities

**Unit 4 (5 hrs)**

**Conflict Resolution**

- 4.1 Reasons for conflict
- 4.2 Consequences of conflict
- 4.3 Managing emotions
- 4.4 Methods of resolving conflicts
- 4.5 Experiential Learning – Based on activities

**Unit 5**

**(5 hrs)**

**Career Mapping**

- 5.1 Goal Setting and Decision Making
- 5.2 Career Planning
- 5.3 Resume Writing
- 5.4 Handling Interviews
- 5.5 Experiential Learning – Based on activities

Workshop on Societal Analysis

**BOOKS FOR REFERENCE**

Khera, Shiv, (2002), **You Can Win**, Macmillan India Ltd., Delhi.

Mishra, Rajiv K., (2004), **Personality Development : Transform Yourself**, Rupa and Co., New Delhi.

Newstrom, John W. and Scannell, Edward E., (1980), **Games Trainers Play: Experiential Learning**, Tata McGraw Hill, New Delhi.

**PATTERN OF EVALUATION (Totally Internal)**

STELLA MARIS COLLEGE (AUTONOMOUS), CHENNAI – 600 086

M.Sc. DEGREE: BRANCH I – MATHEMATICS

SYLLABUS

(Effective from the academic year 2015 – 2016)

**FUZZY SET THEORY AND APPLICATIONS**

CODE : 15MT/PE/FT14

CREDIT: 4

L T P: 4 0 0

TOTAL TEACHING HOURS: 52

**OBJECTIVES OF THE COURSE**

- To introduce the concept of Fuzzy Mathematics
- To cite the applications of Fuzzy Mathematics in various fields

<b>Unit 1</b>		<b>(11 hrs.)</b>
<b>Fuzzy Sets and Operations</b>		
1.1 Fuzzy Sets – Basic Concepts		
1.2 Characteristics and Significance of the Paradigm Shift		
1.3 Operations on Fuzzy Sets		
1.4 Types of Fuzzy Sets		
1.5 Properties of $\alpha$ – cuts		
<b>Unit 2</b>		<b>(10 hrs.)</b>
<b>Properties of Fuzzy Sets</b>		
2.1 Extension Principle for Fuzzy Sets		
2.2 Crisp and Fuzzy Relations – Binary Relations		
2.3 Fuzzy Relational Equations		
<b>Unit 3</b>		<b>(10hrs.)</b>
<b>Operations on Fuzzy Sets</b>		
3.1 Fuzzy Complements		
3.2 Fuzzy Union – fuzzy Intersection – Combination of Operations		
<b>Unit 4</b>		<b>(10 hrs.)</b>
<b>Fuzzy Arithmetic</b>		
4.1 Fuzzy Numbers		
4.2 Linguistic Variables		
4.3 Arithmetic Operation of Fuzzy Intervals		
4.4 Arithmetic Operation of Fuzzy Numbers		
4.5 Fuzzy Equations		

**Unit 5****(11 hrs.)****Applications**

5.1 Concept of Fuzzy Logic

5.2 Fuzzy Controllers

5.3 Application of Fuzzy Logic to Engineering, Medicine, Industry and Electronics

**TEXT BOOKS****UNITS : 1 - 4**

Klir George J. and Yuan Bo, Fuzzy Sets & Fuzzy Logic Theory and Applications, New Delhi : Prentice Hall India, 2009.

Chapter 1 Sections 1.3 – 1.5

Chapter 2 Sections 2.1, 2.3

Chapter 4 Sections 4.1 – 4.4, 4.6

Klir George J. and Folger Tina A., Fuzzy Sets, Uncertainty and Information, New Delhi : Prentice Hall India, 2004.

Chapter 2 Sections 2.2 – 2.5

Chapter 3 Sections 3.1, 3.2, 3.8

**UNIT : 5**

Klir George J. and Yuan Bo, *Fuzzy Sets & Fuzzy Logic Theory and Applications*, New Delhi : Prentice Hall India, 2009.

Terano Toshiro Asai Kiyoji, Sugeno Michio, *Applied Fuzzy Systems*, New York : A.P. Professional, 1994.

**BOOKS FOR REFERENCE**

Cengiz Kahraman, Estronge P.H, *Fuzzy applications in Industrial engineering*, Studies in Fuzziness and soft computing, Springer, 2006.

Huaguang Zhang, *Fuzzy modeling and Fuzzy control*, Control Engineering, Birkhauser, 2006.

John Harris, Nix Eileen, *An Introduction to Fuzzy Logic Applications*, Springer, 2010.

Lotfi A.Zadeh, *Fuzzy Sets and Their Applications to Cognitive and Decision Processes*, New York, Academic Press, 1975.

Michael Hanss, Deshmukh S.K, *Applied Fuzzy Arithmetic*, Springer, 2005.

## WEB RESOURCES

John N. Mordeson, Premchand S. Nair, Fuzzy Mathematics: An Introduction for Engineers and Scientists, Second Edition, Physica-Verlag Heidelberg (2001) ISBN: 3790814202 | 324 pages | PDF | 6.6 MB. e – book

## JOURNALS

Fuzzy Sets and Systems ISSN 0165-0114, Publisher: Elsevier - Netherlands

Iranian Journal of Fuzzy Systems ISSN 1735-0654, Publisher: University of Sistan and Baluchestan

Advances in Fuzzy Mathematics ISSN 0974-0201, Research India Publications

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### End Semester Examination:

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M.Sc. DEGREE: BRANCH I – MATHEMATICS

SYLLABUS

(Effective from the academic year 2015 – 2016)

MECHANICS

CODE: 15MT/PE/ME14

CREDITS: 4

L T P: 4 0 0

TOTAL TEACHING HOURS: 52

### OBJECTIVES OF THE COURSE

- To introduce various principles in dynamical systems
- To teach the techniques involved in calculus of variations
- To formulate equations of motion using different principles

**Unit 1** (10 hrs.)

#### **Elementary Principles of Mechanics, Variational Principles and Lagrange's Equations**

- 1.1 Mechanics of a Particle
- 1.2 Mechanics of a System of Particles – Constraints
- 1.3 D'Alembert's Principle and Lagrange's Equations
- 1.4 Simple Applications of the Lagrangian Formulation
- 1.5 Hamilton's Principle

**Unit 2** (10 hrs.)

#### **Calculus of Variations**

- 2.1 Some Techniques of the Calculus of Variations
- 2.2 Derivation of Lagrange's Equations from Hamilton's Principle
- 2.3 Extension of Hamilton's Principle to Non-holonomic systems
- 2.4 Cyclic Coordinates
- 2.5 General Conservation Theorem Relating to Cyclic Coordinates

**Unit 3** (12 hrs.)

#### **The Kinematics and Equations of Motion of a Rigid Body**

- 3.1 Independent Coordinates of a Rigid Body
- 3.2 Euler Angles – Euler's Theorem on the Motion of a Rigid Body
- 3.3 Rate of Change of a Vector
- 3.4 Coriolis Force
- 3.5 Angular Momentum and Kinetic Energy of Motion about a Point
- 3.6 Eigen Values of Inertia Tensor and Principal Axes Transformation
- 3.7 Euler's Equations of Motion

**Unit 4** (10 hrs.)

**The Hamilton Equations of Motion**

4.1 Legendre Transformations and the Hamilton Equations of Motion

4.2 Routh's Procedure

4.3 Derivation of Hamilton's Equations from a Variational Principle

**Unit 5** (10 hrs.)

**Canonical Transformations**

5.1 Equation of Canonical Transformations - Examples

5.2 Symplectic Approach to Canonical Transformations

**TEXT BOOK**

Goldstein H., *Classical Mechanics* (Reprint 2001), London: Addison – Wesley Publishing Company, 1980.

Chapter 1	Sections 1.1 to 1.4, 1.6.
Chapter 2	Sections 2.1 to 2.4, 2.6
Chapter 4	Sections 4.1, 4.4, 4.6, 4.9, 4.10.
Chapter 5	Sections 5.1,5.4,5.5.
Chapter 8	Sections 8.1, 8.3, 8.5, 8.6
Chapter 9	Sections 9.1 to 9.3

**BOOKS FOR REFERENCE**

Corben, H.C., Stehle Philip, *Classical Mechanics*, (II Edition), New York: Robert E. Krieger Publishing Co., 1960.

Greenwood Donald, T., *Classical Dynamics*, New Delhi: Prentice Hall of India, 1979.

Starzhinskii, V.M., *An Advanced Course of Theoretical Mechanics*, Moscow: MIR Publishers, 1982.

Synge John, L., Byron Griffith, A., *Principles of Mechanics*, (III Edition), New York: McGraw Hill Book Co., 1970.

Venkatachalapathy S.G., *Classical Mechanics*. Chennai: Margham Publications, 2006.

**JOURNALS**

[Journal of Fluid Mechanics / Volume 356 / February 1998, pp 353- 379/Effects of the Coriolis force on the stability of Stuart vortices](#)

[Journal of Applied Mathematics and Mechanics / Canonical Transformations and the Hamilton-Jacobi Theorem in the Optimum Control Theory](#)

## WEB RESOURCES

<http://gsjournal.net/Science-Journals/ResearchPapersMechanicsElectrodynamics>  
[Canonical Transformations in Quantum Mechanics/ scitation.aip.org](http://scitation.aip.org)

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**M.Sc. DEGREE: BRANCH I – MATHEMATICS**

**SYLLABUS**  
**(Effective from the academic year 2015-2016)**

**MATHEMATICAL MODELING**

**CODE: 15MT/PE/MM14**

**CREDITS: 4**

**L T P: 4 0 0**

**TOTAL TEACHING HOURS: 52**

**OBJECTIVES OF THE COURSE**

- To translate real life situations into mathematical models
- To solve problems using mathematical tools

**Unit 1** **(10 hrs.)**

**Traffic Flow Model**

- 1.1 Freeway Traffic
- 1.2 Macroscopic Traffic Flow Models
- 1.3 Conservation of Cars
- 1.4 Traffic Density
- 1.5 Microscopic Traffic Flow Model
- 1.6 Linear Car following Model

**Unit 2** **(10 hrs.)**

**Image Compression: Iterated functions**

- 2.1 Introduction
- 2.2 Affine Transformation in the Plane
- 2.3 Iterated Function Systems
- 2.4 Iterated Contractions and Fixed Points
- 2.5 The Hausdorff Distance
- 2.6 Fractal Dimension
- 2.7 Photographs as Attractions

**Unit 3** **(12 hrs.)**

**The DNA computer**

- 3.1 Introduction
- 3.2 Adlemans Hamiltonian Path Problems
- 3.3 Turing Machines and Recursive Functions
- 3.4 Turing Machines and Insertion Deletion Systems
- 3.5 NP – Complete Problems
- 3.6 DNA Computers

**Unit 4** **(10 hrs.)**

**Nonlinear Difference Equations**

- 4.1 Recognizing a Nonlinear Difference Equation

- 4.2 Steady State Stability and Critical Parameters
- 4.3 The Logistic Difference Equation
- 4.4 Beyond  $r = 3$

**Unit 5**

**(10 hrs.)**

**Application of nonlinear difference equation to population**

- 5.1 Density Dependence in Single Species Population
- 5.2 Two Species Iterations: Host – Parasite Systems
- 5.3 The Nicholson – Bailey Model
- 5.4 Modifications of the NB Model

**TEXT BOOKS**

Clive L. Dym, *Principles of Mathematical Modeling*, Elsevier, India Pvt Ltd, 2006.

Leah Edelstein - Keshet, *Mathematical Models in Biology*, SIAM, Random House, New York, 2005.

Christiane Rousseau and Yvan Sain - Aubin, *Mathematics and Technology*, Translator: Chris Hamilton, Springer science and Business media, L.L.C, 2008.

**BOOKS FOR REFERENCE**

Gershenfeld Neil, *The Nature of Mathematical Modeling*, New York: Cambridge University Press, 1999.

Kapur, J. N., *Mathematical Modeling*, New York: John Wiley & Sons, 1988.

Temam Roger M., Miranville Alain M., *Mathematical Modeling in Continuum Mechanics*, second edition, New York: Cambridge University Press, 2005.

**JOURNALS**

Journal of Mathematical Modelling and Algorithms in Operations Research  
Mathematical Modelling of Natural Phenomena  
Applied Mathematical Modelling Mathematical Modelling and Analysis  
Journal of Mathematical Modelling

**WEB RESOURCES**

<http://libgen.org/>

<http://www.sfu.ca/~vdabbagh/Chap1-modeling.pdf>

[http://www.maths.bris.ac.uk/~madjl/course\\_text.pdf](http://www.maths.bris.ac.uk/~madjl/course_text.pdf)

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SYLLABUS  
(Effective from the academic year 2015 – 2016)

PROBABILITY AND RANDOM PROCESS

CODE: 15MT/PE/PR14

CREDIT : 4

L T P : 4 0 0

TOTAL TEACHING HOURS : 52

OBJECTIVES OF THE COURSE

- To introduce the different techniques of stochastic process and Markov Chains
- To introduce standard concepts and methods of stochastic modeling
- To provide new perspective, methodology, models and intuition and aid in other mathematical and statistical studies

**Unit 1** (12hrs.)

**Random Variables**

1.1 Definition, Discrete, Continuous - Distribution Function, p.d.f, p.m.f.

1.2 Expectation, Moments

**Special probability distributions**

1.3 Binomial, Geometric, Poisson, Uniform

1.4 Exponential, Erlang, Normal

**Unit 2** (12hrs.)

**Multiple Random Variables**

2.1 Joint c.d.f.- Properties-Conditional Distributions

2.3 Conditional Mean - Covariance - Correlation Function

**Unit 3** (12hrs.)

**Introduction to Random Processes**

3.1 Definition, Classification, Characterizing a Random Process

3.2 Cross- correlation, Cross-covariance Functions

3.3 Stationary Random Process- Ergodic Process

3.4 Power Spectral Density- Discrete

3.5 Time Random Process

**Unit 4** (12hrs.)

**Models of Random Processes**

4.1 Bernoulli Process - Random Walk

4.2 Gaussian Process - Poisson Process

**Unit 5**

**(4hrs.)**

**Markov Process**

5.1 Discrete Time Markov Chain

5.2 Continuous Time Markov Chain

**TEXT BOOK**

Oliver, C Ibe. *Fundamentals of Applied Probability and Random Processes*. Elsevier First Indian Reprint 2007

Chapter 2.

Chapter 3: 3.1 to 3.4

Chapter 4: 4.3, 4.4, 4.7 to 4.11

Chapter 5: 5.1 to 5.7

Chapter 8

Chapter 10

**BOOKS FOR REFERENCE**

Basu A.K., *Introduction to Stochastic Processes*, Narosa Publishing House, New Delhi, 2003.

Karlin, S., and H.M. Taylor. *A First Course in Stochastic Processes*, 2<sup>nd</sup> ed., New York: Academic Press, 1975.

Medhi, J. *Stochastic Process*, New York: Wiley Eastern Limited, 1984.

Resnick, Sidney I. *Adventures in Stochastic Processes*, Boston: Birkhauser, 2002.

Taylor H.W., and S. Karlin. *An Introduction to Stochastic Modeling*, 3<sup>rd</sup> ed., New York: Academic Press, 1998.

**JOURNAL**

An International Journal of Probability and Stochastic Processes

Aditi Journal of Probability Theory and Stochastic Processes

AStA Advances in Statistical Analysis

Stochastic Analysis and Applications

ESAIM: Probability and Statistics

## WEB RESOURCES

<http://www.springer.com/statistics/journal/10182>

<http://www.springer.com/statistics/journal/10463>

<http://www.imstat.org/aos/>

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**STELLA MARIS COLLEGE (AUTONOMOUS), CHENNAI – 600 086**  
**Post Graduate Elective Course Offered by Department of Mathematics to students for**  
**M.A., M.Com. & M.Sc. Degree Programme**

**SYLLABUS**  
**(Effective from the academic year 2015 -2016)**

**FORMAL LANGUAGES AND AUTOMATA THEORY**

**CODE: 15MT/PE/FL24**

**CREDITS : 4**

**L T P : 4 0 0**

**TOTAL TEACHING HOURS: 52**

**OBJECTIVES OF THE COURSE**

- To introduce basic concepts of graph theory, formal languages and automata theory
- To enhance compiling techniques and expose to computing device

**Unit 1 (14 hrs.)**

**Graph Theory**

- 1.1 Introduction to Graph Theory, Definition of a Graph and Examples
- 1.2 Degrees and Subgraphs
- 1.3 Isomorphism of Graphs
- 1.4 Matrix Representation of a Graph
- 1.5 Walks, Trails and Paths
- 1.6 Connectedness and Components (concepts only)
- 1.7 Characterisation of Trees
- 1.8 Connectivity of a Graph
- 1.9 Eulerian Graphs (concepts only)
- 1.10 Hamiltonian Graphs (concepts only)

**Unit 2 (10 hrs.)**

**Automata Theory**

- 2.1 Finite Automata (FA) – Introduction and Definition
- 2.2 Representation of Finite Automaton
- 2.3 Acceptability of a String by a Finite Automaton
- 2.4 Language accepted by a Finite Automaton

**Unit 3 (10 hrs.)**

**Automata Theory (contd.)**

- 3.1 Non-deterministic Finite Automata (NFA)
- 3.2 Acceptability of a String by NFA
- 3.3 Equivalence of FA and NFA (concept only)
- 3.4 Procedure for finding an FA equivalent to a given NFA
- 3.5 Properties of Regular Sets (concepts only)

**Unit 4** (12 hrs.)

**Finite State Machines**

- 4.1 Finite-state Machines
- 4.2 The Monoid of a Finite-State Machine
- 4.3 The Machine of a Monoid

**Formal Languages**

- 4.4 Phase-Structure Grammars
- 4.5 Chomsky Hierarchy of Languages
- 4.6 Finite Automata and Regular Languages
- 4.7 Derivation Trees for Content-Free Grammars
- 4.8 Normal Forms for Content free Grammar (concepts only)

**Unit 5** (6 hrs.)

**Project**

- 5.1 Application of Finite Automata and Formal Language
- 5.2 Design of Vending Machine
- 5.3 Document Language Design
- 5.4 Cryptography
- 5.5 DNA Computing

**TEXT BOOKS**

Arumugam S. and Ramachandran S., *Invitation to Graph Theory*, Chennai: Scitech Publications (India) Pvt. Ltd., Reprint December 2013.

- Chapter 1      Sec. 1.1, 1.2
- Chapter 2      Sec. 2.1 – 2.4, 2.8
- Chapter 4      Sec. 4.1, 4.2, 4.4
- Chapter 5      Sec. 5.1, 5.2
- Chapter 6      Sec. 6.1

Venkataraman M.K., Sridharan N., and Chandrasekaran N., *Discrete Mathematics*, Chennai: The National Publishing Company, Reprint 2007.

- Chapter 12    Sec. 1 – 11, 13 – 20

**BOOKS FOR REFERENCE**

Behera, Nayak and Pallnayak, *Formal Languages and Automata Theory*, Vikas Publication, New Delhi, 2014.

Kamala Krithivasan and Rama. R., *Introduction to Formal Languages, Automata Theory and Computation*, Pearson Publishers, Chennai, 2009.

**JOURNALS**

- Formal Languages and Automata Theory
- Journal of Graph Theory
- Discrete Applied Mathematics
- Information Processing Letters

## WEB RESOURCES

<http://www.iitg.ernet.in/dgoswami/Flat-Notes.pdf>

## PATTERN OF EVALUATION

### Continuous Assessment:

**Total Marks: 50**

**Duration: 90 Mins.**

Section A:  $2 \times 2 = 4$  (Two questions to be set)

Section B:  $2 \times 6 = 12$  (Three questions to be set)

Section C:  $2 \times 17 = 34$  (Three questions to be set)

### Third Component :

List of Evaluation Modes:

Seminars

Quiz

Open Book Tests

Group Discussion

Assignments

Project

Theorem Writing Technique

Problem Solving

### End Semester Examination:

**Total Marks: 100**

**Duration: 3 Hours**

Section A :  $5 \times 2 = 10$  (Five questions to be set, selecting one question per unit)

Section B :  $5 \times 6 = 30$  (Seven questions to be set, without omitting any unit)

Section C :  $3 \times 20 = 60$  (Five questions to be set without omitting any unit)

**STELLA MARIS COLLEGE (AUTONOMOUS), CHENNAI - 600 086**

**Post Graduate Elective Course Offered by Department of Mathematics to students for  
M. A. / M. Sc. / M.Com. Degree Programmes**

**SYLLABUS**

**(Effective from the academic year 2015 – 2016)**

**STATISTICS FOR RESEARCH**

**CODE : 15MT/PE/SR34**

**CREDITS: 4**

**L T P: 4 0 0**

**TOTAL TEACHING HOURS: 52**

**ELIGIBILITY CRITERION**

Offered to those who have not studied Statistics in the under graduate programme in the major or allied level

**OBJECTIVES OF THE COURSE**

- To understand and learn research techniques and methodologies
- To acquire basic skills for designing and implementing research projects

**Unit 1 (10 hrs.)**

**Sampling Design**

- 1.1 Implications of a Sample
- 1.2 Characteristics of a Good Sampling Design
- 1.3 Different Types of Sampling Designs
- 1.4 Probability and non-Probability Sampling - Sampling Error
- 1.5 Advantages and Disadvantages of Sampling

**Unit 2 (10 hrs.)**

**Descriptive Statistics**

- 2.1 Methods of Data Collection
- 2.2 Processing and Analysis of Data
- 2.3 Frequency Distribution
- 2.4 Measures of Central Tendency

**Unit 3 (10 hrs.)**

**Descriptive Statistics**

- 3.1 Measures of Dispersion
- 3.2 Normal Distribution
- 3.3 Graphical Representation

**Unit 4 (10 hrs.)**

**Interval Estimation**

- 4.1 Interval Estimation
- 4.2 Concept of Setting Confidence Intervals to Population Parameters

4.3 Confidence Interval for Mean, Difference in Means, Variance, Ratio of Variances based on Normal,  $t$ ,  $\chi^2$  and F Distributions - Simple Problems

**Unit 5**

**(12 hrs.)**

**Tests of Significance**

5.1 Definitions of Statistical Hypothesis - Null and Alternate Hypothesis – Critical Region – Two Types of Errors – Size and Power of a Test - Level of Significance

5.2 Tests of Significance for Large Samples based on Normal,  $t$ ,  $\chi^2$  and F Distributions with regard to Mean, Variance and Coefficient of Correlation

5.3 Tests of Significance for Small Samples based on Normal,  $t$ ,  $\chi^2$  and F Distributions with regard to Mean, Variance and Coefficient of Correlation

5.4  $\chi^2$  test of Goodness of Fit and Independence of Two Attributes – Simple Problems

**TEXT BOOK**

Arora P.N and Arora S., *Statistics for Management*, New Delhi: S. Chand & Company Ltd, 2008.

**BOOKS FOR REFERENCE**

Vital P.R. *Mathematical Statistics*, Chennai : Margam Publications, 2002.

Gupta, S.C. and V.K. Kapoor. *Fundamentals of Mathematical Statistics*, New Delhi: Sultan Chand & Sons, 1979.

Arumugam, S. and Issac. *Statistics*. Palayamkottai : New Gamma Publishing House, 1999.

Kapur J. N. and H.C. Saxena. *Mathematical Statistics*. New Delhi : S. Chand & Co., 1976.

Mood A.M., F.A. Graybill and D.C.Boes. *Introduction of Theory of Statistics*, London: Mc Graw Hill Inc., 1963.

Pillai R.S.N., and V. Bagavathi. *Statistics*. New Delhi : S.Chand Company Ltd., 2000.

Subramaniam N. *Probability and Statistics*. Erode : SCM Publisher, 2005.

Richard I. Levin and David S. Rubin. *Statistics For Management*. New Delhi : Prentice Hall of India Private Ltd., 2000.

**JOURNALS**

The Annals of Statistics

Journal of Computational and Graphical Statistics

## WEB RESOURCES

<http://projecteuclid.org/euclid.aos>

<http://www.tandfonline.com/toc/ucgs20/current#.VO6PrCcas6Yk>

## PATTERN OF EVALUATION

### Continuous Assessment:

**Total Marks: 50**

**Duration: 90 Mins.**

Section A:  $2 \times 2 = 4$  (Two questions to be set)

Section B:  $2 \times 6 = 12$  (Three questions to be set)

Section C:  $2 \times 17 = 34$  (Three questions to be set)

### Third Component :

List of Evaluation Modes:

Seminars

Quiz

Open Book Tests

Group Discussion

Assignments

Project

Theorem Writing Technique

Problem Solving

### End Semester Examination:

**Total Marks: 100**

**Duration: 3 hours**

Section A :  $5 \times 2 = 10$  (One question to be set from each unit)

Section B :  $5 \times 6 = 30$  (Seven questions to be set, without omitting any unit)

Section C :  $3 \times 20 = 60$  (Five questions to be set without omitting any unit)

**STELLA MARIS COLLEGE (AUTONOMOUS), CHENNAI - 600 086**  
**M.Sc. DEGREE : BRANCH I - MATHEMATICS**

**SYLLABUS**

(Effective from the academic year 2015-2016)

**FINANCIAL MATHEMATICS**

(Skill Development Course)

**CODE : 15MT/PI/FM24**

**CREDITS : 4**

**OBJECTIVE OF THE COURSE**

- To introduce mathematical models to enhance the understanding of mathematics of finance and financial markets

**Unit 1**

**Geometric Brownian Motion:**

- 1.1 Geometric Brownian Motion
- 1.2 Geometric Brownian Motion as a Limit of Simpler Models
- 1.3 Brownian Motion - Simple Problems

**Unit 2**

**Interest Rates and Present Value Analysis:**

- 2.1 Interest Rates
- 2.2 Present Value Analysis
- 2.3 Rate of Return
- 2.4 Continuously Varying Interest Rates - Simple Problems

**Unit 3**

**Pricing Contracts via Arbitrage**

- 3.1 An Example in Options Pricing
- 3.2 Other Examples of Pricing via Arbitrage

**The Arbitrage theorem**

- 3.3 The Arbitrage theorem
- 3.4 The Multi-period Binomial Theorem
- 3.5 Proof of the Arbitrage Theorem - Simple Problems

**Unit 4**

**The Black-Scholes Formula**

- 4.1 The Black-Scholes Formula
- 4.2 Properties of Black-Scholes Option Cost
- 4.3 The Delta Hedging Arbitrage Strategy
- 4.4 Some deviations: The Black-Scholes Formula
- 4.5 The Partial Derivatives – Simple Problems

## Unit 5

### Valuing by Expected Utility

- 5.1 Limitations of Arbitrage Pricing
- 5.2 Valuing Investments by Expected Utility
- 5.3 The Portfolio Selection Problem
- 5.4 Value at Risk and Conditional Value at Risk
- 5.5 The Capital Assets Pricing Model
- 5.6 Mean Variance Analysis of Risk-Neutral-Priced Call Options
- 5.7 Rates of Return - Simple Problems

## TEXT BOOK

Sheldon M. Ross. *An Elementary Introduction To Mathematical Finance* 2<sup>nd</sup> ed. Cambridge university press. 2005.

Chapter 3	Sections 3.1 – 3.3
Chapter 4	Sections 4.1 – 4.4
Chapter 5	Sections 5.1 – 5.2
Chapter 6	Sections 6.1 – 6.3
Chapter 7	Sections 7.1 – 7.5
Chapter 9	Sections 9.1 – 9.7

## BOOKS FOR REFERENCE

Joseph. Stampfli, and Victor Goodman, *The Mathematics of Finance Modeling and Hedging*, Thomson publishers

Steven Roman, *Introduction to Mathematics of Finance*, Springer

## JOURNALS

SIAM Journal on Financial Mathematics (SIFIN)

Journal of Mathematical Finance

Journal of Financial Engineering

## WEB RESOURCES

[http://www.tcs.tifr.res.in/~sandeepj/avail\\_papers/chapter.pdf](http://www.tcs.tifr.res.in/~sandeepj/avail_papers/chapter.pdf)

<http://plus.maths.org/content/what-financial-mathematics>

## PATTERN OF EVALUATION: (End Semester Examination - 3 Hours)

Section A:  $10 \times 2 = 20$  (Ten questions to be set selecting two from each unit)

Section B:  $5 \times 8 = 40$  (Seven questions to be set without omitting any unit)

Section C:  $2 \times 20 = 40$  (Three questions to be set without omitting any unit)