

**STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI 600 086**  
(For candidates admitted during the academic year 2009 – 10 & thereafter)

**SUBJECT CODE : MT/PC/ME14**

**M. Sc. DEGREE EXAMINATION, NOVEMBER 2010**  
**BRANCH I - MATHEMATICS**  
**FIRST SEMESTER**

**COURSE : CORE**  
**PAPER : MECHANICS**  
**TIME : 3 HOURS**

**MAX. MARKS : 100**

**SECTION – A**

**( 5 X 8 = 40 )**

**ANSWER ANY FIVE QUESTIONS**

1. Explain Conservation Theorem for the Linear momentum of a system of particles.
2. Explain Brachistochrone problem.
3. Show that twice dissipation function is equal to the rate of energy dissipation.
4. Explain Euler's theorem on the motion of a rigid body.
5. Define moment of inertia and explain with an example.
6. Obtain Lagrange's equations of motion interms of Routhian function.
7. Explain canonical transformation and extended canonical transformation.

**SECTION – B**

**( 3 X 20 = 60 )**

**ANSWER ANY THREE QUESTIONS**

8. a) State and prove D'Alembert's principle.  
b) Give example for the Kinetic energy T be always a homogeneous quadratic form in the generalized velocities.
9. a. Derive Lagrange's Equations from Hamilton's principle.  
b. Explain extension of Hamilton's principle to non-holonomic system.
10. a) State and prove principle of least action.  
b) Define Inertia Tensor and the moment of inertia.
11. a) Derive Hamilton's Canonical equations.  
b) Show that  $Q = \log \left[ \frac{1}{q} \sin p \right], p = qcot p$  is Canonical.
12. a) Obtain algebraic properties of the Poisson bracket.  
b) Show that Poisson bracket and Lagrange bracket are reciprocal to each other.

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