

B.Sc. DEGREE EXAMINATION NOVEMBER 2014
BRANCH III - PHYSICS
THIRD SEMESTER

REG. No. _____

COURSE : MAJOR - CORE

PAPER : MATHEMATICAL PHYSICS

TIME : 30 MINUTES

MAX. MARKS : 30

SECTION – A

TO BE ANSWERED IN THE QUESTION PAPER ITSELF

ANSWER ALL QUESTIONS:

(30x1=30)

Choose the correct answer:

- $\mathbf{a} \cdot \mathbf{b} =$
a) $|\mathbf{a}| |\mathbf{b}| \cos \theta$ b) $|\mathbf{a}| |\mathbf{b}| \sin \theta$ c) $|\mathbf{a}| |\mathbf{b}| \cosh \theta$ d) $|\mathbf{a}| |\mathbf{b}| \sinh \theta$
- The relation between angular velocity $\boldsymbol{\omega}$, linear velocity \mathbf{v} and the position vector \mathbf{r} is given by _____.
a) $\boldsymbol{\omega} = \mathbf{v} \mathbf{r}$ b) $\mathbf{v} = \mathbf{r} / \boldsymbol{\omega}$ c) $\mathbf{v} = \boldsymbol{\omega} \cdot \mathbf{r}$ d) $\mathbf{v} = \boldsymbol{\omega} \times \mathbf{r}$
- If \mathbf{F} is a solenoidal vector function, which of the following condition should be satisfied?
a) $\text{div } \mathbf{F} = 0$ b) $\text{curl } \mathbf{F} = 0$ c) $\int \mathbf{F} \cdot d\mathbf{r} = 0$ d) $\nabla \cdot (\nabla \times \mathbf{F}) = 0$
- The gradient of a scalar field is always a _____.
a) Vector b) scalar c) numeric d) sometimes vector and sometimes scalar
- If $\int_A^B \mathbf{F} \cdot d\mathbf{r}$ is independent of the point joining A and B, then \mathbf{F} is called _____ field.
a) Non- conservative b) Non-lamellar c) Conservative d) Curl
- $L \frac{d^2q}{dt^2} - R \frac{dq}{dt} + \frac{q}{c} = E \sin \omega t$ is a differential equation of _____.
a) degree 1 and order 1 b) degree 1 and order 2
c) degree 2 and order 1 d) degree 2 and order 2
- If m_1 and m_2 are the roots of a differential equation, then the complementary function is
a) $y = (A+Bx)e^{m_1 x}$ b) $y = (A+Bx)e^{m_2 x}$
c) $y = A e^{m_1 x} + e^{m_2 x}$ d) $y = e^{m_1 x}(A \cos m_2 x + B \sin m_2 x)$
- The Legendre equation has singular points _____.
a) 0, ∞ b) $-\infty, \infty$ c) -1, 1 d) 1, 0
- The value of $\frac{2}{3} P_2(x) + \frac{1}{3} P_0(x)$ is _____.
a) x b) x^3 c) $2/3 + x^2$ d) x^2
- $\Gamma(n+1) =$ _____.
a) $n!$ b) $(n+1)!$ c) $(n-1)!$ d) 0

11. The value of $\Gamma(1/2)$ is _____.
- a) π b) $\sqrt{\pi}$ c) ∞ d) 1
12. $\beta(8,9) - \beta(9,8) =$ _____.
- a) 17 b) -1 c) 0 d) 1
13. For a current flowing through an inductance L, the voltage drop across the inductance is _____.
- a) $L^2 \frac{dI}{dt}$ b) $L^2 \left(\frac{dI}{dt}\right)^2$ c) $L \frac{dI}{dt}$ d) $L(d^2I/dt^2)$
14. If x is the displacement of the particle, then its acceleration is _____.
- a) 0 b) $\frac{dx}{dt}$ c) d^2x/dt^2 d) d^2t/dx^2
15. If \mathbf{r} is the position vector, curl \mathbf{r} is _____.
- a) 1 b) 3 c) \mathbf{r} d) 0

State whether the following statements are true or false:

16. The vector product of two vectors is commutative.
17. The work done by a force is a scalar product of two vectors.
18. The physical significance of curl is rotation.
19. $\frac{dy}{dx} + Py = Q$ is called a homogeneous differential equation.
20. $\beta(m,n) = \frac{1}{n} \int_0^\infty e^{-\frac{1}{n}y} dy$.

Fill in the blanks;

21. If the dot product of two vectors is zero, then the vectors are _____ to each other.
22. In the charge free region, the Laplace's equation is _____.
23. A differential equation involving derivatives with respect to a single independent variable is called _____.
24. The value of $P_0(x) =$ _____.
25. The gamma function is defined as _____.

Answer briefly:

26. Write the expression for $\mathbf{a} \times (\mathbf{b} \times \mathbf{c})$.

27. Define divergence of a vector function.

28. Write the equation of continuity in vector form in electromagnetism.

29. Write the Legendre's equation.

30. Find the auxiliary equation of $d^2y/dx^2 - 6(dy/dx) + 9y = 0$

STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI – 600 086.
(For candidates admitted during the academic year 2011-2012 and thereafter)

SUBJECT CODE : 11PH/MC/MP34
B.Sc. DEGREE EXAMINATION NOVEMBER 2014
BRANCH III - PHYSICS
THIRD SEMESTER

COURSE : MAJOR - CORE
PAPER : MATHEMATICAL PHYSICS
TIME : 2 ½ HOURS
MAX. MARKS : 70

SECTION – B

Answer any Five Questions: 5x5=25

1. A force $F = 3i+2j-4k$ is applied at the point $(1,-1,2)$. Find the moment of the force about the point $(2,-1,3)$.
2. If $A = 2xz^2i-yzj+3xz^3k$, find $\nabla \cdot (\nabla \times A)$ at the point $(1,1,1)$.
3. Evaluate $\int_C \mathbf{F} \cdot d\mathbf{r}$ where $\mathbf{F} = xyi+(x^2+y^2)j$ and C is the arc of the curve $y = x^2-4$ from $(2,0)$ to $(4,12)$ in the x - y plane.
4. State Gauss Divergence theorem. Apply the theorem to deduce Gauss law in differential form.
5. Show that for L-R d.c circuit, the current I flowing in the circuit is given by,
$$I = E/R (1 - e^{-\frac{Rt}{L}})$$
6. Evaluate $\int_0^{\infty} \sqrt[4]{x} e^{-\sqrt{x}} dx$.
7. Derive the relation between beta and gamma function.

SECTION – C

Answer any Three Questions: 3x15=45

8. a) Find the angle between the surfaces $x^2+y^2+z^2 = 9$ and $x^2+y^2-z = 3$ at the point $(2,-1, 2)$.
b) If $\frac{d\mathbf{a}}{dt} = \mathbf{u} \times \mathbf{a}$ and $\frac{d\mathbf{b}}{dt} = \mathbf{u} \times \mathbf{b}$, then prove that $\frac{d(\mathbf{a} \times \mathbf{b})}{dt} = \mathbf{u} \times (\mathbf{a} \times \mathbf{b})$.
9. State and prove Stoke's theorem.
10. a) Write the Bernoulli's equation and solve $\frac{dy}{dx} + xy = x^3y^3$.
b) Derive the equation of motion for the free oscillations of a spring.
11. a) Solve the differential equation $d^2x/dt^2 + \frac{g}{l}x = \frac{g}{l}L$
Where g, l, L are constants subject to the conditions $x = a, \frac{dx}{dt} = 0$ at $t = 0$.
b) Solve: $d^2y/dx^2 - 8(dy/dx) + 15y = 0$.
12. Find Rodrigue's formula for Legendre polynomial.
