## STELLA MARIS COLLEGE (AUTONOMOUS), CHENNAI - 86

(For Candidates admitted during the academic year 2011-2012 \& thereafter)
SUBJECT CODE: 11EC/MC/MM14

## B.A. DEGREE EXAMINATION NOVEMBER 2014

BRANCH IV-ECONOMICS
FIRST SEMESTER

## COURSE : MAJOR - CORE <br> PAPER : MATHEMATICAL METHODS FOR ECONOMICS-I <br> TIME : 3 HOURS <br> MAX.MARKS: 100

## SECTION - A

## I. ANSWER ALL QUESTIONS.

(10 X2=20)

1. Show that the lines are parallel

$$
\begin{aligned}
& 4 x-5 y+3=0 \\
& 8 x-10 y \quad=0
\end{aligned}
$$

2. Sketch the illustrative graph of average fixed cost as a function of output.
3. Represent the types of curves according to the value of eccentricity as
(i) $e=1$ (ii) $e>1$
(iii) $\mathrm{e}<1$.
4. Write down the equation of ellipse.
5. Solve: $\operatorname{Lt}_{x \rightarrow-1} \frac{x^{2}+4 x+3}{x^{2}-7 x-8}$
6. Find dy/dx: $y=x^{3} e^{3 x}$
7. Find second order differentiation: $y=32 x^{3}$
8. If the MR is Rs. 25 and the elasticity of demand with respect to price is Rs.2, find AR?
9. Find partial derivatives: $Z=\frac{5 x^{2}}{5 x-y+4}$
10. The total revenue ( R ) and total cost $(\mathrm{C})$ functions of a firm are given by:
$R=30 \mathrm{Q}-\mathrm{Q}^{2} ; \mathrm{C}=20+4 \mathrm{Q}$, Where Q is the output, Find the equilibrium output of the firm.

## SECTION - B

## II. ANSWER ANY FIVE QUESTIONS.

11. (i) Convert 120 into radians.
(ii) Express 0.1815 into degrees.
(iii) Find the co-ordinates of midpoint of the line joining $(-3,4)$ and $(7,-7)$
(iv) Plot a point $(3,4)$ and find the distance from origin.
12. Find the co-ordinates of the focus and the directrix of the parabola for the given equations
(i) $y^{2}=4 x+4 y$
(ii) $\mathrm{x}^{2}+4 \mathrm{x}+2 \mathrm{y}=0$.
13. Trace the following curve and then find their vertex, focus and directrix

$$
y^{2}-4 y+4 x=0
$$

14. Find the value of limits: (1) $\operatorname{Lt} \underset{x \rightarrow 0}{ } \frac{\sqrt{x}+1-1}{x}$

$$
\underset{x \rightarrow \infty}{\text { (2) } \operatorname{Lt} \frac{\sqrt{x}+1-1}{x}}
$$

15. (1) Let $Y=3 x^{2}+9 x+8$ and $Z=x^{3}+10$. Evaluate the derivatives with respect to $x$ at $x=1$ as $\mathrm{Z} / \mathrm{Y}$.
(2) Find dy/dx in the following: $y=10^{x}+\log (2 x+1)+x^{2}-6$
16. Diagrammatically explain the conditions for profit maximization.
17. A monopolist firm has the following total cost and demand functions:
$\mathrm{C}=\mathrm{aQ} \mathrm{Q}^{2}+\mathrm{bQ}+\mathrm{c} \quad ; \mathrm{P}=\beta-\alpha Q$. What is the profit maximizing output level when the firm is assumed to fix the output?

## SECTION - C

III. ANSWER ANY TWO QUESTIONS.
$(2 \mathrm{X} 20=40)$
18. Find all the second order partial derivatives of the following:
(a) $Z=\frac{x+4}{2 x+5 y}$
(b) $\mathrm{Z}=\mathrm{x}^{3} \mathrm{e}^{2 y}$
19. (i) Plot a point (2,-4.8). Drop perpendiculars $A B$ and $A C$ to the $x$-axis and $y$-axis respectively. Calculate the lengths of the diagonals of OBAC.
(ii) Find the intercepts on axes of x and y for the following: $2 \mathrm{x}-4 \mathrm{y}-3=0$.
(iii) Find the equation of a circle which passes through 3 point: $(0,1),(5,1),(2,-3)$.
20. Discuss the function of a function rule and explain with illustration.
21. Graphically explain the three stages of production function.

