STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI 600 086 (For candidates admitted during the academic year 2011 – 12)

SUBJECT CODE : 11MT/PC/ME14

M. Sc. DEGREE EXAMINATION, NOVEMBER 2011 BRANCH I - MATHEMATICS FIRST SEMESTER

COURSE	:	CORE
PAPER	:	MECHANICS
TIME	:	3 HOURS

MAX. MARKS: 100

(5 X 2 = 10)

(5X 6 = 30)

SECTION – A ANSWER ALL THE QUESTIONS

- 1. Define generalized coordinates.
- 2. Explain Lagrange undetermined multipliers.
- 3. Define Dyad.
- 4. State modified Hamilton's Principle.
- 5. Define Canonical Transformation.

SECTION – B ANSWER ANY FIVE QUESTIONS

- 6. Define Holonomic Constraint with an example.
- 7. State and prove Hamilton's Principle.
- 8. Obtain the moment of Inertia about the axis of rotation.
- 9. Explain Coriolis Force.
- 10. Obtain Lagrangian equations interms of Routhian function.
- 11. Obtain Hamilton's Canonical equations of motions.
- 12. State and prove Jacobi' identity relating Poisson Brackets.

$SECTION - C \qquad (3X20 = 60)$ ANSWER ANY THREE QUESTIONS

- 13. a) State and Prove D'Alemberr's Principle.
 - b) Explain principle of virtual work.
- 14. a) Obtain the standard form of Lagrange's Equations for a non-holonomic system.
 - b) Obtain Lagrange equation for a hoop rolling, without slipping, down an inclined plane.
- 15. State and prove principle of least action.
- 16. Show that for any point in a rigid body one can find a set of Cartesian axes for which the inertia tensor I will be diagonal and obtain secular equation.
- 17. a) Obtain canonical equations of motion for the major four generating functions.

b) Show that the transformation $Q = \log \frac{\sin p}{q}$, $P = q \cot p$ is canonical.
