

**B. Com. DEGREE EXAMINATION, NOVEMBER 2011  
COMMERCE  
THIRD SEMESTER**

**COURSE : ALLIED – CORE**

**PAPER : MATHEMATICS FOR COMMERCE**

**TIME : 3 HOURS**

**MAX. MARKS : 100**

**SECTION – A**

**(10 X 2 = 20)**

**ANSWER ALL THE QUESTIONS**

1. Show that the matrix  $\begin{pmatrix} 0 & 1+i \\ -1+i & 0 \end{pmatrix}$  is skew Hermitian.
2. Prove that the inverse of an orthogonal matrix is orthogonal.
3. Show that the matrix  $\begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{i}{\sqrt{2}} \\ -i & -1 \end{pmatrix}$  is unitary.
4. If  $\alpha, \beta, \gamma$  are the roots of the equation  $x^3 + px^2 + qx + r = 0$ , Find the value of  $\sum \alpha^2$ .
5. Form the quadratic equation one of whose roots is  $1+2i$
6. Define interpolation.
7. Write Lagrange's formula for interpolation.
8. Find  $\frac{dy}{dx}$  if  $x^2 + y^2 = 4ax$
9. Find the second derivative of  $\frac{1}{(ax+b)^2}$
10. Evaluate  $\int \frac{dx}{x^2 + x + 6}$

**SECTION – B**

**(5 X 8 = 40)**

**ANSWER ANY FIVE QUESTIONS**

11. Find the eigen values and eigen vectors of the matrix  $\begin{pmatrix} 4 & 1 \\ 3 & 2 \end{pmatrix}$
12. Solve the equation  $x^3 - 12x^2 + 39x - 28 = 0$  whose roots are in A.P.

13. Solve the equation  $x^4 - 10x^3 + 26x^2 - 10x + 1 = 0$ .

14. A function  $f(x)$  is given by the following table. Find  $f(0.2)$  using a suitable formula.

$x$	0	1	2	3	4	5	6
$f(x)$	176	185	194	203	212	220	229

15. Using Lagrange's formula, Find  $y(10)$  from the following table.

$x$	5	6	9	11
$Y$	12	13	14	16

16. Find  $\frac{dy}{dx}$  if  $xy + xe^{-y} + ye^x = x^2$

17. Evaluate  $\int x \sin^2 x dx$

### SECTION – C

(2 X 20 = 40)

### ANSWER ANY TWO QUESTIONS

18. a) Using Cayley Hamilton theorem, Find the inverse of the matrix  $\begin{pmatrix} 1 & 3 & 7 \\ 4 & 2 & 3 \\ 1 & 2 & 1 \end{pmatrix}$

b) Find the eigen values and eigen vectors of the matrix  $\begin{pmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{pmatrix}$

(10+10)

19. a) Solve the equation  $x^3 + x^2 - 16x + 20 = 0$ , given that the difference between two of its roots is 7.

b) Find the values of  $y$  at  $x = 28$  from the following data.

$x$	20	23	26	29
$y$	.342	.3907	.4384	.4848

(10+10)

20. a) Find the differential coefficient of  $\frac{(1-x)\sqrt{x^2+2}}{(x+3)\sqrt{x-1}}$

b) Evaluate  $\int \frac{1}{3x^2 + 13x - 10} dx$ .

c) Evaluate  $\int \frac{4x-3}{x^2+3x+8} dx$ .

(6+5+9)



