

STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI – 86
(For candidates admitted from the academic year 2023 – 2024 and thereafter)

B.C.A. DEGREE EXAMINATION, NOVEMBER 2024
THIRD SEMESTER

COURSE : **ALLIED CORE**
PAPER : **MATHEMATICS FOR COMPUTER SCIENCE-1**
SUBJECT CODE : **23MT/AC/MS35**
TIME : **3 HOURS** **MAX. MARKS: 100**

Q. No.	SECTION A (5 × 2 = 10) Answer ANY FIVE questions	CO	KL
1.	Find the eigen values of the matrix $\begin{bmatrix} 1 & 2 \\ 5 & 4 \end{bmatrix}$.	1	1
2.	Find the unit vector normal to $\phi = x^2 - y^2 + z$ at (1, -1, 2).	1	1
3.	Define solenoidal vector.	1	1
4.	Write Newton-Raphson formula to obtain the cube root of N.	1	1
5.	Define numerical differentiation and numerical integration	1	1
6.	Define slack and surplus variables in LPP	1	1

Q. No.	SECTION B (10 × 1 = 10) Answer ALL questions	CO	KL
7.	Cayley-Hamilton theorem can be verified for which type of matrix? a) column matrix b) row matrix c) square matrix d) zero matrix	2	2
8.	Given a matrix $A = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$, which of the following is the characteristic equation of A? a) $\lambda^2 + 2\lambda + 1 = 0$ b) $\lambda^2 + 2\lambda - 1 = 0$ c) $(\lambda - 1)^2 = 0$ d) $\lambda^2 - 2\lambda = 0$	2	2
9.	For a vector field \vec{f} , if $\nabla \cdot \vec{f} = 0$, then the vector field is _____ a) rotational b) solenoidal c) irrotational d) Scalar potential	2	2
10.	If $\phi(x, y, z) = x^2 + y^2 + z^2$ is a scalar function, what is grad ϕ ? a) (2x, 2y, 2z) b) (x, y, z) c) (2, 2, 2) d) (0, 0, 0)	2	2
11.	How does the bisection method determine the next interval? a) By taking the derivative of the function. b) By evaluating the function at multiple points. c) By finding the midpoint of the current interval. d) By randomly selecting points in the interval.	2	2

12.	What does the Gauss elimination process convert a system into? a) A triangular matrix. b) A diagonal matrix. c) A row-reduced matrix. d) A symmetric matrix.	2	2
13.	For Newton's forward interpolation, which term is used to represent the first difference? a) Δy_0 b) y_0 c) $\Delta^2 y_0$ d) $\Delta^3 y_0$	2	2
14.	To estimate a value using Newton's backward interpolation, what is the formula for the first backward difference ∇y_n ? a) $\nabla y_n = y_n - y_{n+1}$ b) $\nabla y_n = y_{n+1} - y_n$ c) $\nabla y_n = y_n - y_{n-1}$ d) $\nabla y_n = y_n + y_{n-1}$	2	2
15.	Which of the following is NOT a requirement for a linear programming problem? a) The objective function must be linear b) All variables must be non-negative c) Constraints can be non-linear d) All constraints must be expressed as linear inequalities or equations	2	2
16.	What is the feasible solution in linear programming? a) A solution that maximizes the objective function b) A solution that satisfies all constraints c) A solution that minimizes the objective function d) A solution that includes all possible variable values	2	2

Q. No.	SECTION C (2 × 15 = 30) Answer ANY TWO questions	CO	KL																					
17.	Verify Cayley Hamilton theorem for $\begin{bmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 2 & 0 & 3 \end{bmatrix}$ and find its inverse.	3	3																					
18.	Using bisection method, find a real root of the equation $x^3 - x - 11 = 0$.	3	3																					
19.	Obtain the first and second derivatives of $y = \log_e x$ from the following data <table border="1" style="margin-left: 20px;"> <tr> <td>x</td> <td>500</td> <td>510</td> <td>520</td> <td>530</td> <td>540</td> <td>550</td> </tr> <tr> <td>y</td> <td>6.214</td> <td>6.234</td> <td>6.253</td> <td>6.272</td> <td>6.291</td> <td>6.309</td> </tr> <tr> <td>$= \log_e^x$</td> <td>6</td> <td>4</td> <td>8</td> <td>9</td> <td>6</td> <td>9</td> </tr> </table> <p>(i) at $x = 500$ by Newton's forward difference formula and (ii) at $x = 550$ by Newton's backward difference formula.</p>	x	500	510	520	530	540	550	y	6.214	6.234	6.253	6.272	6.291	6.309	$= \log_e^x$	6	4	8	9	6	9	3	3
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20.	Apply Simplex method to find the non negative values of x, y and z which <i>Maximize</i> $Z = 3x + 2y + 5z$ Subject to $x + 4y \leq 420$ $3x + 2z \leq 460$ $x + 2y + z \leq 430, x, y, z \geq 0$	3	3																					

Q. No.	SECTION D (2 × 15 = 30) Answer ANY TWO questions	CO	KL																								
21.	Diagonalize the matrix $\begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$	4	4																								
22.	If $\phi = \frac{x}{r^3}$, $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$ and $r = \vec{r} $, then prove that (i) $div \vec{r} = 3$. (ii) $curl \vec{r} = 0$. (ii) $\nabla^2 \phi = 0$.	4	4																								
23.	Solve the following system of linear equations by Gauss Jordan method $\begin{aligned} x + y + z &= 9 \\ 2x - 3y + 4z &= 13 \\ 3x + 4y + 5z &= 40 \end{aligned}$	4	4																								
24.	A company manufactures 2 types of printed circuits. The requirements of transistors, resistors and capacitors for each type of printed circuits along with other data are given below <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th></th> <th colspan="2">Circuit</th> <th>Stock available</th> </tr> <tr> <th></th> <th>A</th> <th>B</th> <th></th> </tr> </thead> <tbody> <tr> <td>Transistor</td> <td>15</td> <td>10</td> <td>180</td> </tr> <tr> <td>Resistor</td> <td>10</td> <td>20</td> <td>200</td> </tr> <tr> <td>Capacitor</td> <td>15</td> <td>20</td> <td>210</td> </tr> <tr> <td>Profit</td> <td>Rs.5</td> <td>Rs.8</td> <td></td> </tr> </tbody> </table> <p>Determine, how many circuits of each type should the company produce from the stock to earn maximum profit by graphical method ?</p>		Circuit		Stock available		A	B		Transistor	15	10	180	Resistor	10	20	200	Capacitor	15	20	210	Profit	Rs.5	Rs.8		4	4
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Q. No.	SECTION E (2 × 10 = 20) Answer ANY TWO questions	CO	KL
25.	If $\phi = x^3 + y^3 + z^3 - 3xyz$, find $div grad\phi, curl grad\phi$.	5	5
26..	Evaluate $\int_0^5 \frac{dx}{4x+5}$ by Trapezoidal rule using 11 coordinates.	5	5
27.	Evaluate $\sqrt{12}$ to four decimal places by Newton-Raphson method.	5	5

28.	<p>a) Express the following LPP in standard matrix form Maximize $Z = 4x_1 + 2x_2 + 6x_3$ Subject to $2x_1 + 3x_2 + 2x_3 \geq 6$ $3x_1 + 4x_2 = 8$ $6x_1 - 4x_2 + x_3 \leq 10$ and $x_1, x_2, x_3 \geq 0$</p> <p>b) A firm produces three product. These products are processed on three different machines. The time required to manufacture one unit of each of the three products and the daily capacity of the three machines are given in the table below:</p> <table border="1" data-bbox="391 542 1204 806"> <thead> <tr> <th rowspan="2">Machine</th> <th colspan="3">Time per unit (minutes)</th> <th rowspan="2">Machine capacity (Minutes/day)</th> </tr> <tr> <th>Product 1</th> <th>Product 2</th> <th>Product 3</th> </tr> </thead> <tbody> <tr> <td>M_1</td> <td>2</td> <td>3</td> <td>2</td> <td>440</td> </tr> <tr> <td>M_2</td> <td>4</td> <td>-</td> <td>3</td> <td>470</td> </tr> <tr> <td>M_3</td> <td>2</td> <td>5</td> <td>-</td> <td>430</td> </tr> </tbody> </table> <p>It is required to find the number of units to be manufactured for each product daily. The profit per unit for product 1,2, 3 is Rs.4, Rs.3, Rs. 6 respectively. It is assumed that all the amounts produced are consumed in the market. Formulate the mathematical model for the problem. (5+5)</p>	Machine	Time per unit (minutes)			Machine capacity (Minutes/day)	Product 1	Product 2	Product 3	M_1	2	3	2	440	M_2	4	-	3	470	M_3	2	5	-	430	5	5
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