

STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI – 600 086.  
(For candidates admitted during the academic year 2011-12)

SUBJECT CODE : 11PH/MC/MP34  
B.Sc. DEGREE EXAMINATION NOVEMBER 2012  
BRANCH III - PHYSICS  
THIRD SEMESTER

REG. No. \_\_\_\_\_

COURSE : MAJOR – CORE  
PAPER : MATHEMATICAL PHYSICS  
TIME : 30 MINS.

MAX. MARKS : 30

SECTION – A

TO BE ANSWERED IN THE QUESTION PAPER ITSELF

ANSWER ALL QUESTIONS:

(30x1=30)

I CHOOSE THE CORRECT ANSWER:

- $k \times i =$   
a)  $i \times k$       b)  $k$       c)  $i$       d)  $-i \times k$
- $a \cdot b =$   
a)  $ab$       b)  $ab \sin \theta$       c)  $ab \cos \theta$       d)  $ab \sin \theta \hat{n}$
- $\text{curl grad } \phi =$   
a) 0      b)  $\infty$       c) 1      d) -1
- Integral of a point function along a curve is called  
a) surface integral      b) line integral      c) volume integral
- $\text{div } J =$   
a)  $\frac{d\rho}{dt}$       b)  $\frac{dP}{dt}$       c)  $\frac{-d\rho}{dt}$       d)  $\frac{-dP}{dt}$
- Two vectors are collinear if and only if  $a \times b =$   
a)  $\infty$       b) 1      c)  $\frac{\pi}{2}$       d) 0
- The differential equation whose solution is  $y = a \cos(x + 3)$  is  $\frac{dy}{dx} =$  \_\_\_\_\_  
a)  $y \tan(x + 3)$       b)  $y \sec(x + 3)$       c)  $-y \tan(x + 3)$       d)  $-y \sec(x + 3)$
- A coil of resistance  $15\Omega$  and inductance  $10\text{H}$  is connected to a  $10\text{V}$  supply. The value of current after  $2 \text{secs}$  is ( $e^{-3} = 0.05$ )  
a)  $6\text{A}$       b)  $5\text{A}$       c)  $4\text{A}$       d)  $7\text{A}$
- Voltage drop across capacitance is  
a)  $v/c$       b)  $c/v$       c)  $q/v$       d)  $q/c$
- The auxiliary equation for  $\frac{d^2y}{dx^2} + P \frac{dy}{dx} + Q = 0$  is  
a)  $m^2 + Pm + Q = 0$       b)  $\frac{1}{m^2} + \frac{P}{m} + Q = 0$       c)  $(Pm + Q)^2$       d)  $m(P + Q)^2$

..2..

11. The solution to equation  $\frac{d^2y}{dx^2} + \mu^2y = 0$  is  $y =$   
 a)  $C_1 \cos \mu x$       b)  $C_1 \sin \mu x$       c)  $C_1 \cos \mu x + C_2 \sin \mu x$       d)  $\frac{\cos \mu x + \sin \mu x}{C_1 + C_2}$
12. The voltage gradient of a transmission line from the transmitted end is expressed as  
 a)  $dv/dt$       b)  $-dv/dt$       c)  $dv/dx$       d)  $-dv/dx$
13.  $\Gamma_0 =$  \_\_\_\_\_  
 a)  $\infty$       b) 0      c) 1      d) -1
14.  $\beta_{(m,n)} =$  \_\_\_\_\_  
 a)  $\Gamma_m \Gamma_n \Gamma_{(m+n)}$       b)  $\Gamma_m / \Gamma_{m+n}$       c)  $\Gamma_{m+n} / \Gamma_m \Gamma_n$       d)  $\Gamma_m \Gamma_n / \Gamma_{m+n}$
15.  $P_0(x) =$  \_\_\_\_\_  
 a) 0      b)  $\infty$       c) 1      d) -1

## II. FILL IN THE BLANKS:

16. If  $s$  is a scalar function of  $t$ , then  $\frac{dx}{dt} =$  \_\_\_\_\_
17.  $\text{curl curl } A =$  \_\_\_\_\_
18.  $\frac{dy}{dx} + p(x)y = f(x)$  is a differential equation of \_\_\_\_\_ order.
19. For an equation  $D^2 + K^2 = 0$ ,  $D =$  \_\_\_\_\_
20.  $\Gamma_{n+1} =$  \_\_\_\_\_

## III. STATE WHETHER TRUE OR FALSE:

21.  $i \cdot i = 1$ .
22.  $\text{Curl } A = \nabla \cdot A$
23. The rate at which ice melts is proportional to the amount of ice at that instant.
24. Complete solution = Complementary function + Particular integral.
25.  $\Gamma_1 = 1$

**IV.ANSWER THE FOLLOWING:**

26. What is the expression for the moment of a force.
27. Give the statement for Stoke's theorem.
28. State any one application for first order differential equation.
29.  $A = 2i + 3j + 4k$  and  $B = 3i - 4j + k$  find A.B.
30.  $\Gamma_{\frac{1}{2}} =$

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COURSE : MAJOR – CORE  
PAPER : MATHEMATICAL PHYSICS  
TIME : 2 ½ HOURS

MAX. MARKS : 70

SECTION – B

ANSWER ANY FIVE QUESTIONS:

(5x5=25)

1. If for two vectors  $\vec{a}$  and  $\vec{b}$ ,  $|\vec{a} + \vec{b}| = |\vec{a} - \vec{b}|$ . Find the angles between  $\vec{a}$  and  $\vec{b}$ .
2. A fluid motion is given by  $\vec{v} = (y \sin z - \sin x)i + (x \sin z + 2yz)j + (xy \cos z + y^2)k$ . Is the motion rotational or irrotational?
3. Uranium disintegrates at a rate proportional to the amount present at any instant. If  $m_1$  and  $m_2$  grams of uranium are present at time  $t_1$  and  $t_2$  respectively. Show that half life of uranium is  $\frac{(t_1 - t_2) \log^2}{\log \frac{m_1}{m_2}}$ .
4. State  $\frac{d^2y}{dx^2} - 8 \frac{dy}{dx} + 15y = 0$
5. State and prove Green's theorem.
6. Evaluate  $\int_0^\infty \sqrt[4]{x} e^{-\sqrt{x}} dx$ .
7. Show that  $\Gamma_n \Gamma_{1-n} = \frac{\pi}{\sin n\pi}$  ( $0 < n < 1$ )

SECTION – C

ANSWER ANY THREE QUESTIONS:

(3x15=45)

8. If  $r$  is the distance of a point  $(x, y, z)$  from the origin prove that

$$\text{curl} \left( k \times \text{grad} \frac{1}{r} \right) + \text{grad} \left( k \cdot \text{grad} \frac{1}{r} \right) = 0$$

Where  $k$  is the unit vector in the direction OZ.

9. State and prove divergence theorem of Gauss.
10. A body falling vertically under gravity encounters resistance of the atmosphere. If the resistance varies as the velocity show that  $\frac{du}{dt} = g - ku$  where  $u$  is the velocity,  $k$  is a constant and  $g$  is acceleration due to gravity. Show that as  $t$ , increase  $u$  approaches the value  $g/k$ . Also if  $u = \frac{dx}{dt}$  where  $x$  is the distance fallen by the body from rest in time  $t$ , show that  $x = \frac{gt}{k} - \frac{g}{k^2} (1 - e^{-kt})$ .
11. Find expressions for current in a series circuit containing
  - i) L and R
  - ii) L, C and R
12. Deduce the Rodrigue's formula for legendre polynomial  
$$P_n(x) = \frac{1}{2^n n!} \frac{d^n}{dx^n} (x^2 - 1)^n$$

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