STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI - 600086
(For candidates admitted from the academic year 2023-2024)

## M. Sc. DEGREE EXAMINATION, APRIL 2024 <br> BRANCH III - PHYSICS <br> SECOND SEMESTER

| COURSE | : MAJOR CORE |  |
| :--- | :--- | :--- |
| PAPER | $:$ MATHEMATICAL PHYSICS - II |  |
| SUBJECT CODE | $: 23$ PH/PC/MP24 |  |
| TIME | $: 3$ HOURS | MAX. MARKS: 100 |


| Q. No. | SECTION A (Answer ALL Questions) | CO | KL |
| :---: | :---: | :---: | :---: |
| 1. | Find L[ $\cos \omega t$ ]. | CO1 | K1 |
| 2. | Find the Fourier sine transform of $1 / \mathrm{x}$ | CO1 | K1 |
| 3. | Express Laplace's equation in two dimensional cylindrical coordinates ( $\mathrm{r}, \theta$ ). | CO1 | K1 |
| 4. | What is the one dimensional wave equation? | CO2 | K2 |
| 5. | What is orthogonality of Bessel's function? | CO2 | K2 |
| 6. | Define Hankel functions of first kind. | CO 2 | K2 |
| 7. | Distinguish isomorphism and homomorphism of the group. | CO2 | K2 |
| 8. | What do you mean by cosets? | CO3 | K3 |
| 9. | Define Standard deviation and write its formula. | CO3 | K3 |
| 10. | State binomial theorem of probability | CO3 | K3 |
| Q. No. | SECTION B $6 \times 5=30 \text { Marks }$ | CO | KL |
|  | PART - A  <br> Answer Any TWO Questions $(2 \times 5=10)$ |  |  |
| 11. | Evaluate $L^{-1}\left\{\frac{3 s-2}{s^{3}\left(s^{2}+4\right)}\right\}$ | CO3 | K3 |
| 12. | Show that $H_{n}(-x)=(-1)^{n} H_{n}(x)$ | CO3 | K3 |
| 13. | The mean and variance of binomial distribution are 8 and 6 . Find $P(x \geq 2)$. | CO3 | K3 |
|  | PART - B Answer Any FOUR Questions $\quad(4 \times 5=20)$ |  |  |
| 14. | State and prove Convolution theorem. | CO4 | K4 |
| 15. | Solve the differential equation $\frac{\partial u}{\partial t}=\frac{\partial^{2} u}{\partial x^{2}}$, if $\mathrm{u}(\mathrm{x}, 0)=\sin \Pi \mathrm{x}$. | CO4 | K4 |
| 16. | Prove $x J_{n}{ }^{\prime}(x)=n J_{n}(x)-x J_{(n+1)}(x)$ | CO4 | K4 |
| 17. | Describe character table and Construct the character table for $\mathrm{C}_{2 \mathrm{v}}$ point group. | CO4 | K4 |
| 18. | The radius of a wire is measured in cm as $0.17,0.15,0.18$, $0.19,0.16,0.17$. Find the mean radius and the standard deviation. | CO4 | K4 |


| Q. No. | SECTION C  <br> Answer ALL Questions  $\mathbf{2 \times 2 0 = 4 0 \text { Marks }}$ | CO | KL |
| :---: | :---: | :---: | :---: |
| 19. | (i) a. Find the Laplace transform of sawtooth wave function $f(t)=\frac{a t}{T}$ for $0<t<T$ and $f(t+T)=f(t)$. | CO5 | K5 |
|  | b. Find the finite sine and cosine transform of $f(x)=$ $\sin a x$ | CO5 | K6 |
|  | (OR) |  |  |
|  | (ii) a. Obtain the solution of wave equation by D'Alembert's method. | CO5 | K5 |
|  | b. Applying method of variable separation to solve the solution for three dimensional heat flow equation. | CO5 | K6 |
| 20. | (i) a. Obtain the complete solution for Bessel differential equation. | CO5 | K5 |
|  | b. Prove the orthogonality of Hermite polynomial. | CO5 | K6 |
|  | (OR) |  |  |
|  | (ii) a. State and prove Orthogonality theorem of characters in group theory. | CO5 | K5 |
|  | b. Explicate Poisson's distribution and calculate its mean and moment generating function. | CO5 | K6 |

