STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI - 600086
(For candidates admitted from the academic year 2023 - 2024)
B. A DEGREE EXAMINATION, APRIL 2024

## BRANCH IV - ECONOMICS

SECOND SEMESTER

| COURSE | $:$ ALLIED CORE |
| :--- | :--- |
| PAPER | $:$ MATHEMATICAL METHODS FOR ECONOMICS |
| COURSE CODE | $:$ 23EC/AC/MM25 |
| TIME | $: 3$ HOURS |


| Q. No. | SECTION-A PART - A <br> Answer all TEN questions Each answer not to exceed 50 words. <br> ( $10 \times 2=20$ ) | CO | KL |
| :---: | :---: | :---: | :---: |
| 1 | Find the slope of the points (1, -2) and ( $3,-6$ ). | 1 | 1 |
| 2 | Find the equation of the line passing through the points ( $1,-1$ ) and (2, -4). | 1 | 1 |
| 3 | What is a Scalar Matrix? | 1 | 1 |
| 4 | Define Input-Output Analysis? | 1 | 1 |
| 5 | Find $\frac{d y}{d x}$ of $\mathrm{y}=e^{4 x^{2}}$. | 1 | 1 |
| 6 | Calculate the limit for $\lim _{x \rightarrow-4} 3 x^{2}+7 x-12$ | 1 | 1 |
| 7 | If AC $=2 \mathrm{x}+1-\frac{5}{x}$, Find TC and MC. | 1 | 1 |
| 8 | Comment if the Matrix A $=\left[\begin{array}{ll}1 & 2 \\ 3 & 4\end{array}\right]$ is singular or nonsingular? | 1 | 1 |
| 9 | If $\mathrm{Q}=0.6 \mathrm{~K}^{2}-3 \mathrm{KL}+\mathrm{L}^{2}$, Find $\mathrm{MP}_{\mathrm{L}}$ and $\mathrm{MP}_{\mathrm{K}}$ | 1 | 1 |
| 10 | Illustrate the shape of the Average Cost. | 1 | 1 |
| Q. No. | Part - B <br> Answer any TEN questions. Each answer not to exceed 50 words. $(10 \times 2=20)$ | CO | KL |
| 11 | Find the equilibrium price and quantity from the data given $Q_{s}=-20+3 P$ and $Q_{d}=220-5 P$ | 2 | 2 |
| 12 | Solve for x from the following linear equation $36-4 x=7 x-34$ | 2 | 2 |
| 13 | If $A=\left[\begin{array}{ll}6 & 7 \\ 2 & 3\end{array}\right] \quad B=\left[\begin{array}{cc}-6 & 2 \\ 4 & -8\end{array}\right]$, Find $A+B$. | 2 | 2 |
| 14 | State the meaning of a Quadratic Function with an example. | 2 | 2 |


| 15 | If $\mathrm{y}=\log 2 \mathrm{x}$, Find dy/dx. | 2 | 2 |
| :---: | :---: | :---: | :---: |
| 16 | Define Price Elasticity of Demand. | 2 | 2 |
| 17 | Find the MR function from the following Demand function $\mathrm{Q}=36-2 \mathrm{P}$. | 2 | 2 |
| 18 | Differentiate $\mathrm{y}=(7 \mathrm{x}+9)^{2}$ | 2 | 2 |
| 19 | State Hawkins Simon Conditions. | 2 | 2 |
| 20 | Find the determinant of $\mathrm{A}=\left[\begin{array}{cc}18 & -1 \\ -2 & 36\end{array}\right]$ | 2 | 2 |
| 21 | Find the distance of a point $\mathrm{P}(4,3)$ from the origin. | 2 | 2 |
| 22 | State any two properties of Parallel Lines. | 2 | 2 |
| Q. No. | $\begin{aligned} & \text { SECTION - B } \\ & \text { PART - A } \end{aligned}$ <br> Answer any FOUR questions. Each answer not to exceed 250 words. $(4 \times 5=20)$ | CO | KL |
| 23 | Optimize $\mathrm{f}(\mathrm{x})=2 \mathrm{x}^{3}-30 \mathrm{x}^{2}+126 \mathrm{x}+59$ and state whether the function is at a relative maximum or relative minimum. | 3 | 3 |
| 24 | Illustrate the Input-Output Transaction Matrix. | 3 | 3 |
| 25 | Prove Young's Theorem for $\mathrm{z}=\mathrm{x}^{0.3} \mathrm{y}^{0.5}$ | 3 | 3 |
| 26 | Find the Inverse of the Matrix $A=\left[\begin{array}{lll}4 & 2 & 5 \\ 3 & 1 & 8 \\ 9 & 6 & 7\end{array}\right]$ | 3 | 3 |
| 27 | Suppose the demand function for a certain good is given by $\mathrm{Q}=100-2 \mathrm{P}+0.5 \mathrm{I}-0.3 \mathrm{PC}$, where Q is the quantity demanded, P is the price of the good, I is income, and PC is the price of a related good. <br> Find the income elasticity of demand $\left(\mathrm{E}_{\mathrm{I}}\right)$ for this good and calculate the cross elasticity of demand $\left(\mathrm{E}_{\mathrm{PC}}\right)$ with respect to the price of the related good. | 3 | 3 |
| 28 | Differentiate $y=\frac{18 x^{2}}{x^{2}-1}$ | 3 | 3 |


| Q. No. | PART - B | CO | KL |
| :---: | :---: | :---: | :---: |
|  | Answer any FOUR questions. Each answer not to exceed 250 words. <br> $(4 \times 5=20)$ |  |  |
| 29 | Find the Minors and Cofactors of for the elements of the first row $A=\left[\begin{array}{ccc} 5 & 2 & -4 \\ 6 & -3 & 7 \\ 1 & 2 & 4 \end{array}\right]$ | 4 | 4 |
| 30 | Solve by Cramer's Rule $\begin{aligned} & 2 x+4 y-z=52 \\ & -x+5 y+3 z=72 \\ & 3 x-7 y+2 z=10 \\ & \hline \end{aligned}$ | 4 | 4 |
| 31 | Find $\frac{d y}{d x}$ for the function $7 x^{4}+3 x^{3} y+9 x y^{2}=280$ | 4 | 4 |
| 32 | Given $\mathrm{Y}=\mathrm{C}+\mathrm{I}$, when $\mathrm{C}=89+0.8 \mathrm{Y}$ and $\mathrm{I}_{0}=24$, Find the Equilibrium Level of Income. | 4 | 4 |
| 33 | For $\mathrm{z}=\mathrm{f}(\mathrm{x}, \mathrm{y})=6 \mathrm{x}^{3}+7 \mathrm{y}$ where $\mathrm{y}=\mathrm{g}(\mathrm{x})=4 \mathrm{x}^{2}+3 \mathrm{x}+8$, Find the total derivative $\frac{d z}{d x}$. | 4 | 4 |
| 34 | Derive the relationship when $\mathrm{AC}>\mathrm{MC}$. | 4 | 4 |
| Q. No. | SECTION - C <br> Answer any TWO questions. Each answer not to exceed 600 words. $(2 \times 10=20)$ | CO | KL |
| 35 | Given the following functions, $\mathrm{C}=100+0.8 \mathrm{Y}, \mathrm{I}=120-5 \mathrm{i}$, $\mathrm{M}_{\mathrm{s}}=120$, <br> $\mathrm{M}_{\mathrm{d}}=0.2 \mathrm{Y}-5 i$, Find the equilibrium income and interest rate. | 5 | 5 |
| 36 | List any 5 properties of determinants with examples. | 5 | 5 |
| 37 | Calculate the maximum profit from the information provided $\mathrm{TR}=5900 \mathrm{Q}-10 \mathrm{Q}^{2}$ and $\mathrm{TC}=2 \mathrm{Q}^{3}-4 \mathrm{Q}^{2}+140 \mathrm{Q}+845$ | 5 | 5 |
| 38 | Consider an economy with three sectors: Agriculture (A), Manufacturing (M), and Services (S). The input-output matrix representing the relationships between these sectors is given by: $\left[\begin{array}{c} A \\ S \\ M \end{array}\right]=\left[\begin{array}{lll} 0.3 & 0.2 & 0.1 \\ 0.4 & 0.5 & 0.3 \\ 0.3 & 0.3 & 0.6 \end{array}\right]$ <br> Determine the total output generated by each sector when Rs. 500 worth of final output is produced. | 5 | 5 |

