STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI - 600086 (For candidates admitted from the academic year 2023-2024)

## M.A DEGREE EXAMINATION, NOVEMBER 2023

BRANCH III - ECONOMICS
FIRST SEMESTER
COURSE : ELECTIVE
PAPER : MATHEMATICS FOR ECONOMICS
SUBJECT CODE: 23EC/PE/ME15
TIME : 3 HOURS MAX. MARKS: 100

| Q. No. | SECTION A <br> PART $-A \quad(2 \times 5=10)$ <br> Answer any TWO out of THREE questions in about 150 <br> words each | CO | KL |
| :---: | :---: | :---: | :---: |
| 1 | Find the inverse of A $\left[\begin{array}{cc} 7 & 9 \\ 6 & 12 \end{array}\right]$ | 1 | 1 |
| 2 | Find the First and second order Direct Partial Derivatives $Z=13 x^{2}+6 x y+9 y^{3}$ | 1 | 1 |
| 3 | If Average Cost $=12 t^{2}-18 t+28$ Find TC and MC. | 1 | 1 |
| Q. No. | PART - B (2 X 5 = 10) <br> Answer any TWO out of THREE questions in about 150 <br> words each | CO | KL |
| 4 | Explain the concepts of Slack and Surplus Variables. | 2 | 2 |
| 5 | Evaluate $\int_{2}^{4}\left(5 x^{3}+2 x^{2}+3 x\right) d x$ | 2 | 2 |
| 6 | Find $\mathrm{dy} / \mathrm{dx}$ of $4 \mathrm{x}^{3}-\mathrm{y}^{3}=97$ | 2 | 2 |
| Q. No. | \[\) SECTION B  <br>  PART -  A \(\quad(2 \times 8=16)\]Answer any TWO out of THREE questions in about 400 <br> words each | CO | KL |
| 7 | Solve by Cramer's Rule : $\begin{array}{ll} 5 x_{1}-2 x_{2}+3 x_{3} & =16 \\ 2 x_{1}+3 x_{2}-5 x_{3} & =2 \\ 4 x_{1}-5 x_{2}+6 x_{3} & =7 \end{array}$ | 3 | 3 |


| 8 | Determine the sign definiteness for matrix A $\left[\begin{array}{cc} 10 & 3 \\ 3 & 4 \end{array}\right]$ | 3 | 3 |
| :---: | :---: | :---: | :---: |
| 9 | Derive Samuelson's Multiplier Accelerator model. | 3 | 3 |
| Q. No. | PART - B $\quad(2 \times 8=16)$ <br> Answer any TWO out of THREE questions in about 400 words each | CO | KL |
| 10 | Solve by the Graphical method <br> Minimize $C=20 x+40 y$ <br> Subject to the Constraints $36 x+6 y \geq 108$ $\begin{aligned} & 3 x+12 y \geq 36 \\ & 20 x+10 y \geq 100 \\ & \text { Where } x, y \geq 0 \end{aligned}$ | 4 | 4 |
| 11 | Find the Second order direct Partial Derivatives $Z=(7 x+3 y)^{3}$ | 4 | 4 |
| 12 | The technology matrix of an economic system with two industries is $\left[\begin{array}{ll} 0.50 & 0.30 \\ 0.41 & 0.33 \end{array}\right]$ <br> Test whether the system is viable as per the Hawkins-Simon Condition. | 4 | 4 |
|  | SECTION C <br> PART - A $\quad(2 \times 12=24)$ <br> Answer any TWO out of FOUR questions in about 700 <br> words each |  |  |
| 13 | Find the profit maximizing level of output, price and profit $\begin{aligned} & \mathrm{Q}_{1}=5200-10 \mathrm{P}_{1} \\ & \mathrm{Q}_{2}=8200-20 \mathrm{P}_{2} \\ & \mathrm{C}=0.1 Q_{1}^{2}+0.1 \mathrm{Q}_{1} \mathrm{Q}_{2}+0.2 Q_{2}^{2}+325 \end{aligned}$ | 5 | 5 |
| 14 | Determine the total demand for industries 1,2 and 3, given the matrix of technical coefficients A and the final demand vector $B$. $A=\left[\begin{array}{lll} 0.4 & 0.3 & 0.1 \\ 0.2 & 0.2 & 0.3 \\ 0.2 & 0.4 & 0.2 \end{array}\right] \quad B=\left[\begin{array}{l} 140 \\ 220 \\ 180 \end{array}\right]$ | 5 | 5 |
| 15 | Enumerate the various applications of Linear Programming | 5 | 5 |


| 16 | Calculate the General Solution of the differential equation <br> dy/dt $+3 \mathrm{t}^{2} \mathrm{y}=\mathrm{t}^{2}$ | $\mathbf{5}$ | $\mathbf{5}$ |
| :--- | :--- | :--- | :--- |
|  | Answer any TWO out of FOUR questions in about 700 <br> words each | PART $\mathbf{~ B ~}$ |  |
| 17 | Given the demand function $\mathrm{P}_{\mathrm{d}}=113 \mathrm{Q}^{2}$ and the Supply <br> function $\mathrm{P}_{\mathrm{s}}=(\mathrm{Q}+1)^{2}$ under Pure Competition, Find <br> Consumers' and Producers' Surplus. | $\mathbf{6}$ | $\mathbf{6}$ |
| 18 | A monopolistic firm has the following demand functions for <br> each of its products x and y <br> $\mathrm{x}=72-0.5 \mathrm{P}_{\mathrm{x}}$ | $\mathbf{6}$ | $\mathbf{6}$ |
| 19 | $\mathrm{y}=120-\mathrm{P}_{\mathrm{y}}$ <br> The combined cost function is c $=\mathrm{x}^{2}+\mathrm{xy}+\mathrm{y}^{2}+35$ and the <br> maximum joint production is 40. Find the profit maximizing <br> level of output, price and profit. | Construct an Input -Output Transaction Table and list the <br> limitations of Input -Output analysis. | $\mathbf{6}$ |
| 20 | Examine the features of Solow Growth Model. | $\mathbf{6}$ | $\mathbf{6}$ |

