

STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI - 600 086
(For candidates admitted during the academic year 2019–20 and thereafter)

B. Sc. DEGREE EXAMINATION, NOVEMBER 2023
BRANCH I - MATHEMATICS
THIRD SEMESTER

COURSE : MAJOR – CORE
PAPER : DIFFERENTIAL EQUATIONS
SUBJECT CODE : 19MT/MC/DE34
TIME : 3 HOURS **MAX. MARKS : 100**

SECTION-A

Answer any TEN questions

(10 x 2 = 20)

1. Solve $x^2 \frac{d^2y}{dx^2} + 3x \frac{dy}{dx} + y = 0$.
2. Solve $x^2 \frac{d^2y}{dx^2} - 3x \frac{dy}{dx} + 4y = 0$.
3. Solve $\frac{dx}{yz} = \frac{dy}{xz} = \frac{dz}{xy}$.
4. Solve $\frac{dx}{-y^2-z^2} = \frac{dy}{xy} = \frac{dz}{xz}$.
5. A 4 lb weight is attached to a spring whose spring constant is 16 lb/ft. What is the period of simple harmonic motion?
6. Solve $\frac{1}{8}x'' + 8x = 0$.
7. Solve by eliminating the constants a and b from the equation $z = (x + a)(y + b)$.
8. Solve $x^2p + y^2q = z^2$.
9. Solve $\frac{\partial^2z}{\partial x^2} + a^2 \frac{\partial^2z}{\partial y^2} = 0$.
10. Solve $r - 4s + 4t = 0$.
11. Calculate the particular integral for $(D^2 + 4)y = xe^{2x}$.
12. Solve $z = px + qy + p^2 + q^2$.

SECTION-B

Answer any FIVE questions

(5 x 8 = 40)

13. Solve $(D^2 - 4D + 3)y = e^{-x} \sin x$.
14. Solve $\frac{dx}{mz-ny} = \frac{dy}{nx-lz} = \frac{dz}{ly-mx}$.
15. An 8 lb weight stretches a spring 2 ft. Assuming that a damping force numerically equal to 2 times the instantaneous velocity acts on the system, determine the equation of motion if the weight is released from the equilibrium position with an upward velocity of 3ft/s.

16. Solve $(y^2 + z^2 - x^2)p - 2xyq + 2xz = 0$.

17. Solve $\frac{\partial^2 z}{\partial x^2} - \frac{\partial^2 z}{\partial y^2} = x - y$.

18. Solve $x^2 \frac{d^2 y}{dx^2} + 8x \frac{dy}{dx} + 12y = x^4$.

19. Solve $p^2 + q^2 = x + y$.

SECTION-C

Answer any TWO questions

(2 x 20 = 40)

20. (a) Solve $\frac{d^2 y}{dx^2} + n^2 y = \sec nx$ by the method of variation of parameter. (10 marks)

(b) Find the differential equation from $\varphi(x + y + z, x^2 + y^2 + z^2) = 0$ (10 marks)

21. (a) Solve the equations (10 marks)

$$2 \frac{dx}{dt} + x + \frac{dy}{dt} = \cos t$$

$$\frac{dx}{dt} + 2 \frac{dy}{dt} + y = 0$$

(b) Solve $(D' - 6DD' + 9D'^2) = 12x^2 + 36xy$. (10 marks)

22. (a) Find the solution of the initial value problem (10 marks)

$$\frac{d^2 y}{dx^2} = \frac{w}{T_1} \left(1 + \left(\frac{dy}{dx} \right)^2 \right)^{\frac{1}{2}}$$

$$y(0) = \frac{T_1}{w}, y'(0) = 0.$$

(b) Solve $x^2(y - z)p + y^2(z - x)q = z^2(x - y)$. (10 marks)

