STELLA MARIS COLLEGE (AUTONOMOUS), CHENNAI - 600086 (For Candidates admitted during the academic year 2019-2020 \& thereafter)

SUBJECT CODE: 19EC/AC/MM25

## B.A. DEGREE EXAMINATION APRIL 2023 BRANCH IV - ECONOMICS SECOND SEMESTER

## COURSE : ALLIED - CORE

PAPER : MATHEMATICAL METHODS FOR ECONOMICS TIME : 3 HOURS

MAX.MARKS: 100

## SECTION A

## ANSWER ANY TEN QUESTIONS.

$(10 \times 2=20)$

1. Find the slope of the curve $2 x=-4 y+5$
2. Find the equation of the hyperbola whose centre is $(6,2)$ and focus is
$(4,2) \quad \mathrm{e}=2$.
3. If $\mathrm{A}=\left[\begin{array}{lll}2 & 1 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9\end{array}\right]$ Find [A|
4. Find AB and BA , if $\int 46$
$\mathrm{A}=\left(\begin{array}{lll}4 & 6 & 2 \\ 1 & 2 & 4 \\ 3 & 9 & 2\end{array}\right)$ and $\mathrm{B}=\left(\begin{array}{l}8 \\ 7 \\ 1\end{array}\right)$
5. What is logarithmic function?
6. If $Z=15 y^{2}$ and $Y=2 x^{2}$, Find $d z / d x$.
7. Write down the derivation of Margi al cost function.
8. Find out the elasticity of demand for the following functions:

$$
\text { i) } P=x e^{x} \quad \text { ii) } P=x e^{-x}
$$

9. Find the Maximum and Minimum values of the function $Y=x^{2}-6 x+13$
10. The cost C of manufacturing a certain article is given by formula $C=5+48 / x+3 x^{2}$ where $x$ is the number of article manufactured. Find Minimum value of C .
11. Find the partial derivatives of $Z=4 x^{2}+4 x y+y^{2}$
12. Given $Z=x^{2}-2 x+2 y^{2}$, Find $(\partial z / \partial x)$ and $(\partial z / \partial y)$

## SECTION B

## ANSWER ANY FIVE QUESTIONS.

$(5 \times 8=40)$
13. Given the price line $2 x+3 y=20$. Find the slope and $y$-Intercept.
14. Find inverse of the matrix
$\left[\begin{array}{ccc}1 & 1 & -4 \\ -1 & -2 & 1 \\ 2 & 4 & -5\end{array}\right]$
15. If $U=X^{3}+Y^{3}+Z^{3}-3 X Y Z$, Prove that $X(\partial u / \partial x)+Y(\partial u / \partial y)+Z(\partial u / \partial z)=3 U$
16. Write down the rules of differentiation.
17. Examine the properties of determinants.
18.The total profit $Y$ (in rupees) of a company from the manufacture and sale of $x$ bottles is given by $y=-x^{2} / 400+2 x-80$ :
i) How many bottles must the company sell to achieve maximum profit?
ii) What is the profit per bottle when this maximum is achieved?
19. For the supply function $x=5+2 p^{2}$. Find the elasticity of the supply at $\mathrm{p}=2$.
20. Show that $f(x, y, z)=(x / z)+(y / z)$ is homogenous function in $x, y, z$ of zero degree.

## SECTION C

## ANSWER ANY TWO QUESTIONS.

$(2 \times 20=40)$
21. Find the equation of the Straight line, If $y$ intercept is -7 and slope is $3 / 4$.
22. Solve the following set of Linear equation simultaneous equations:

$$
\begin{align*}
2 x_{1}+3 x_{2} & =5  \tag{1}\\
11 x_{1}-5 x_{2} & =6 \tag{2}
\end{align*}
$$

23. The total cost $C(x)$ associated with producing and marketing $X$ units of an item is given by $C(x)=0.005 x^{3}-0.02 x^{2}-30 x+3000$. Find
(i) Total cost when output is 4 units
(ii) Average cost of output of 10 Units.
(iii) Marginal cost when the output is 3 Units.
24. Find the maximum and minimum values of $2 x^{3}-3 x^{2}-36 x+10$
