

M.A. DEGREE EXAMINATION NOVEMBER 2022  
BRANCH III – ECONOMICS  
FIRST SEMESTER

COURSE : ELECTIVE  
PAPER : MATHEMATICS FOR ECONOMICS  
TIME : 3 HOURS

MAX. MARKS: 100

SECTION – A

ANSWER ANY FIVE QUESTIONS IN 300 WORDS:

(5 x 8 = 40)

1.a) If  $A = \begin{pmatrix} 2 & 1 \\ 4 & 3 \end{pmatrix}$  and  $AB = \begin{pmatrix} 7 & 3 \\ 15 & 5 \end{pmatrix}$  Find B?

b) State the Limitations of Input-Output analysis.

2. The total cost C is given by  $C = 0.015x^3 - 0.03x^2 + 20x + 2000$  Find

- Total cost when output=5
- AC when output x=8
- MC when output x=4.

3. Optimize function  $z = 4x^2 + 3xy + 6y^2$  subject to the constraint  $x + y = 56$ .

4. Explain the Formulation of the Dual Programme.

5. Integrate  $2x+5 / (x^2+4x+5)$

6. Determine the rank matrix

$$A = \begin{pmatrix} -3 & 6 & 2 \\ 1 & 5 & 4 \\ 4 & -8 & 2 \end{pmatrix}$$

7. Solve the following differential equations

a)  $d^2y/dx^2 - 6dy/dx + 8y = e^{2x}$       b)  $d^2x/dt^2 - 4dx/dt + 3x = 0$

SECTION – B

ANSWER ANY THREE QUESTIONS IN 1200 WORDS:

(3 x 20=60)

8.a) Find the Inverse of  $\begin{pmatrix} 2 & 3 & 4 \\ 3 & 2 & 1 \\ 1 & 1 & -2 \end{pmatrix}$

b) Solve by matrix method  
 $2x+4y+z=5$ ,  $x+y+z=6$ ,  $2x+3y+z=6$

9. a) If the demand law is  $p = (4-5x)^2$ , in what value of x, the elasticity of demand is unity.

b) Find all the first and second order partial derivatives with respect to x and y of the function  $u = x^3 + y^3 - 3xy$ .

10. a) Given the utility function  $U=10x+20y-x^2-y^2+2xy$  where  $x$  and  $y$  are the commodities consumed. Find out the total differential  $dU$ .
- b) A monopolistic firm has the following demand function for each of the products  $x$  and  $y$ .  $x=72-0.5P_x$  and  $y=120-P_y$ . The combined cost function is  $C= x^2+xy+y^2+35$  and maximum joint production is 40. Thus  $x+y=40$ . Find the profit maximizing level of  
 a) Output b) price and c) profit.
11. Solve the L.P.P  
 Maximise  $Z= 2x_1+3x_2$   
 S.To  $x_1+x_2 \leq 30$   
 $x_2 \geq 3$ ,  
 $0 \leq x_2 \leq 12$ ,  
 $x_1 -x_2 \geq 0$ ,  
 $0 \leq x_1 \leq 20$ .
12. The demand and supply laws are  $P_d= (6-x)^2$  and  $P_s=14+x$  respectively. Find the consumer's surplus, if  
 i) the demand and price are determined under pure competition and  
 ii) the demand and price are determined under monopoly and supply function is identified with the marginal cost function.

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