STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI - 600086 (For candidates admitted from the academic year 2019-20 \& thereafter)

## SUBJECT CODE : 19MT/AC/ST45

## B. Sc. DEGREE EXAMINATION, APRIL 2022 <br> BRANCH I - MATHEMATICS <br> FOURTH SEMESTER

## COURSE : ALLIED CORE <br> PAPER : MATHEMATICAL STATISTICS - II TIME : 3 HOURS

MAX. MARKS : 100

> SECTION - A

## ANSWER ANY TEN QUESTIONS:

$(10 \times 2=20)$

1. Write two mathematical properties of Regression coefficients.
2. If $r=0.99$, find the regression equation for the following data

|  | X | Y |
| :--- | :---: | :---: |
| Average | 7.6 | 14.8 |
| Standard deviation | 3.6 | 2.5 |

3. What is called sampling? Give one example.
4. Write down two assumptions on $t$-test.
5. State any two characteristics of Chi-square test.
6. Write down $95 \%$ confidence limits for the true mean $\mu$ determined from large sample.
7. Define Fisher's $F$-test.
8. Mention any two applications of $F$-test.
9. What is called Linear trend in time series analysis?
10. Express additive model of time series analysis in terms of its components.
11. What is called ANOVA?
12. The trend of annual production of a company is described by $y_{c}=18+0.6 X$ with origin 2007;
$X$-unit $=1$ year ; $Y$ unit $=$ annual production. Convert the equation to a monthly trend equation.

## SECTION - B

## ANSWER ANY FIVE QUESTIONS:

13. Find the mean of variables of $X$ and $Y$ and the correlation coefficient from the following regression equations: $2 Y-X-50=0 ; 3 Y-2 X-10=0$. Estimate $X$ when $Y=20$.
14. A machine puts out 16 imperfect articles in a sample of 500 . After the machine is overhauled, it puts out 3 imperfect articles in a batch of 100 . Has the machine improved?
15. Productivity test of two food articles- Paddy and Wheat gives the following results:

|  | Average yield (tonnes) | S.D | No. of hectares |
| :--- | :---: | :---: | :---: |
| Paddy | 80 | 10 | 120 |
| Wheat | 75 | 12 | 90 |

Is the difference between standard deviation significant?
16. Differentiate between point estimation and interval estimation. Obtain the $95 \%$ confidence limits for population parameter $\lambda$ of the Poisson distribution $f(x, \lambda)=\frac{e^{-\lambda} \lambda^{x}}{x!}$. (2+6)
17. In a sample of 8 observations, the sum of squared deviations of items from the mean was 94.5. In another sample of 10 observations, the value was found to be 101.7. Test whether the difference is significant at $5 \%$ level.
18. Explain briefly about four components of Time series analysis.
19. Assuming a four-yearly cycle, calculate the trend by the method of moving averages from the following data relating to the production of tea in India.

| Year | 1998 | 1999 | 2000 | 2001 | 2002 | 2003 | 2004 | 2005 | 2006 | 2007 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Production (in <br> million lbs) | 464 | 515 | 518 | 467 | 502 | 540 | 557 | 571 | 586 | 612 |

## SECTION - C

## ANSWER ANY TWO QUESTIONS:

20. a) Calculate the regression equations of X on Y and Y on X from the following data:

| Sales | 91 | 97 | 108 | 121 | 67 | 124 | 51 | 73 | 111 | 57 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Purchases | 71 | 75 | 69 | 97 | 70 | 91 | 39 | 61 | 80 | 47 |

b) The heights of six randomly chosen soldiers are in inches : 76, 70, 68, 69, 69 and 68. Those of 6 are randomly chosen sailors are 68, 64, 65, 69, 72 and 64. Discuss in the light of these data throw on the suggestions that soldiers are, on the average, taller than sailors, Use t -test.
21. a) From the data given below about the treatment of 250 patients suffering from a disease, state whether the new treatment is superior to the conventional treatment:

| Type of treatment | No. of patients |  |
| :--- | :---: | :---: |
|  | Favourable | Not Favourable |
| New | 140 | 30 |
| Conventional | 60 | 20 |

(Given at $5 \%$, chi-square value is 3.84 , for 1 d.f, and 7.81 for 3 d.f ).
b) Fit a parabola of the second degree to the data given below:

| Year | 2003 | 2004 | 2005 | 2006 | 2007 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Sales\{ $\left.{ }^{\circ} 000\right)$ | 16 | 18 | 19 | 20 | 24 |

(8+12)
22. Perform a two way analysis of variance on the data given below:

| Plots of Land | A | B | C | D |
| :---: | :---: | :---: | :---: | :---: |
| I | 50 | 40 | 48 | 39 |
| II | 46 | 48 | 50 | 45 |
| III | 39 | 44 | 40 | 39 |

(Use coding method subtracting 40 from the given numbers)

