

STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI-86  
(For candidates admitted during the academic year 2019-20& thereafter)

SUBJECT CODE: 19CH/PC/QG24

M.Sc. DEGREE EXAMINATION, APRIL 2021

BRANCH IV - CHEMISTRY

SECOND SEMESTER

COURSE: MAJOR CORE

PAPER: QUANTUM CHEMISTRY AND GROUP THEORY

TIME: 90 minutes

MAX.MARKS:50

SECTION-A

Answer all the questions

(11 x 1 = 11 Marks)

I. Choose the correct answer:

1. Which among the following is a well-behaved wave function?

- a)  $e^{x^2}$       b)  $e^x$       c)  $e^{-x}$       d)  $e^{i\theta}$

2. The zero point energy of a particle in a one-dimensional box is:

- a) 0      b)  $h^2/8ma^2$       c)  $3h^2/8ma^2$       d)  $h^2/8m^2a^2$

3. The Hermite polynomial for n=1 is:

- a)  $4q^2$       b) 1      c)  $2q^2-2$       d) 2q

4. Identify the molecule which does not possess a centre of symmetry

- a) 1,4-dichloro-2,5-difluorobenzene    b) dichloromethane    c) staggered ferrocene  
d) benzene

II Fill in the blanks:

5. The commutator for  $[\widehat{L}_x, \widehat{L}_y]$  is \_\_\_\_\_

6. The conjugate of  $\sigma_{xz}$  in  $C_{2v}$  point group is \_\_\_\_\_

7. The symmetry of vibrational ground state of water molecule is \_\_\_\_\_

8. In the character table of  $C_{3v}$  point group, there are \_\_\_\_\_ one dimensional IRR  
and \_\_\_\_\_ two dimensional IRR.

III Answer in a line or two:

9. What is a rigid rotator with fixed axis?

10. Determine the position of the node on the r-axis for the 2s orbital of Hydrogen atom.

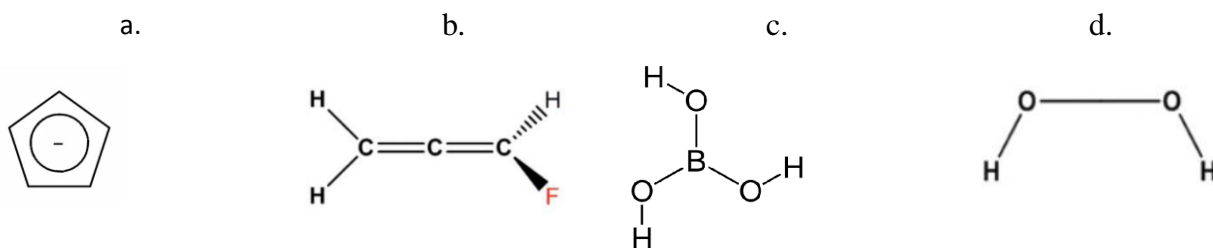
11. Prove that reflections through planes perpendicular to each other commute.

## SECTION – B

Answer any three questions

(3x8=24 marks)

12. Explain HMO treatment to 1,3-butadiene and arrive its wave function and energy.
13. a) Prove that the operators  $\hat{A}$  and  $\hat{B}$  do not commute with each other for the function  $\sin x$  and also prove that the commutator is a unit operator. [4]
- b) The eigen value for a particle confined to move in a 3D box is  $17h^2/8ma^2$ . Determine the quantum numbers  $n_x, n_y, n_z$  and the degree of degeneracy. [4]
14. a) In the electronic spectrum of Formaldehyde, the  $\pi$  to  $\pi^*$  transition is symmetry allowed, while the  $n$  to  $\pi^*$  is symmetry forbidden. Explain the above statement using Group theory. [6]
- b) Explain the Symmetry operations: rotations and reflections in methane molecule. [2]
15. Identify the point groups of the following compounds and give their symmetry elements, order and number of classes.



## SECTION – C

Answer any One question

(1x15=15 marks)

16. a) Prove that the angular momentum of rigid rotator is quantised. [3]
- b) Apply perturbation theory to helium atom and determine the first order perturbation correction energy for the ground state. [8]
- c) Write the character table of  $C_{2v}$  point group. [4]
17. a) Determine the position of the node on the  $r$  axis for the  $3p$  orbital of the  $Be^{3+}$  ion. [3]
- b) Derive the ground state and excited state wave functions of He atom and prove that the electrons are paired in one excited state and parallel in three excited states. [9]
- c) Show that  $H_2O$  molecule belongs to abelian group whereas  $NH_3$  molecule belongs to non-abelian group. [3]

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