STELLA MARIS COLLEGE (AUTONOMOUS) CHENNAI 600086 (For candidates admitted during the academic year 2015-16\& thereafter)

SUBJECT CODE : 15MT/ME/OT55

## B. Sc. DEGREE EXAMINATION, NOVEMBER 2018 <br> BRANCH I - MATHEMATICS <br> FIFTH SEMESTER

COURSE : MAJOR - ELECTIVE
PAPER : OPTIMIZATION TECHNIQUES TIME : 3 HOURS

MAX. MARKS :100
SECTION - A
(10X2=20)

## ANSWER ALL THE QUESTIONS

1. Define slack variable.
2. Define Model.
3. Define feasible solution in Transportation Problem.
4. Define Unbalanced assignment problem.
5. Define Total elapsed time.
6. State the conditions for processing of n jobs through three machines.
7. Define saddle point.
8. Define pure strategy.
9. Define Activity.
10. Define Project.

## SECTION - B <br> ANSWER ANY FIVE QUESTIONS

(5X8=40)
11. Solve graphically Maximize $Z=100 x_{1}+40 x_{2}$
subject to $5 x_{1}+2 x_{2} \leq 1000,3 x_{1}+2 x_{2} \leq 900, x_{1}+2 x_{2} \leq 500$
$x_{1}, x_{2} \geq 0$
12. Find IBFS for the given transportation problem by VAM rule.

|  |  | To |  | supply |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| From | 21 | 16 | 25 | 13 | $\mathbf{1 1}$ |
|  | 17 | 18 | 14 | 23 | $\mathbf{1 3}$ |
|  | 32 | 27 | 18 | 41 | $\mathbf{1 9}$ |
| Demand | $\mathbf{6}$ | $\mathbf{1 0}$ | $\mathbf{1 2}$ | $\mathbf{1 5}$ |  |

13. Obtain the optimal sequence that minimize the total elapsed time for the jobs given below

| Job: | $\mathbf{a}$ | $\mathbf{b}$ | $\mathbf{c}$ | $\mathbf{d}$ | $\mathbf{e}$ | $\mathbf{f}$ | $\mathbf{g}$ | $\mathbf{h}$ | $\mathbf{I}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | ---: |
| M1: | 2 | 5 | 4 | 9 | 6 | 8 | 7 | 5 | 4 |
| M2: | 6 | 8 | 7 | 4 | 3 | 9 | 3 | 8 | 11 |

14. Solve the following game $\left[\begin{array}{cc}2 & -1 \\ -1 & 6\end{array}\right]$.
15. A maintenance activities consists of eight jobs .Draw the network . find the critical path and total float for each activity.

| Job: | $1-2$ | $2-3$ | $3-4$ | $3-7$ | $4-5$ | $4-7$ | $5-6$ | $6-7$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Duration: $\begin{array}{lllllllll}3 & 4 & 4 & 4 & 2 & 2 & 3 & 2\end{array}$
16. Solve the following Travelling salesman problem.

To city
$\begin{array}{lllll}1 & 2 & 3 & 4 & 5\end{array}$
$\begin{array}{cc}\text { From city } & 1 \\ & 2 \\ & 3 \\ & 4 \\ & 5\end{array}\left[\begin{array}{rcccc}- & 10 & 25 & 25 & 10 \\ 1 & - & 10 & 15 & 2 \\ 8 & 9 & - & 20 & 10 \\ 14 & 10 & 24 & - & 15 \\ 10 & 8 & 25 & 27 & -\end{array}\right]$
17. Explain the some applications of Operations research.

$$
\begin{gathered}
\text { SECTION - C } \\
\text { ANSWER ANY TWO QUESTIONS }
\end{gathered}
$$

(2X20=40)
18. a) Solve by Big-M method Minimize $Z=12 x_{1}+20 x_{2}$ subject to $6 x_{1}+8 x_{2} \geq 100,7 x_{1}+12 x_{2} \geq 120$ $x_{1}, x_{2} \geq 0$
b) Solve the given Assignment problem

|  | I | II | III | IV | V |
| :---: | :---: | :---: | :---: | :---: | :---: |
| A | 10 | 5 | 9 | 18 | 11 |
| B | 13 | 9 | 6 | 12 | 14 |
| C | 3 | 2 | 4 | 4 | 5 |
| D | 18 | 9 | 12 | 17 | 15 |
| E | 11 | 6 | 14 | 19 | 10 |

19. a) There are 6 jobs each of which is to be processed through 3 machines $\mathrm{A}, \mathrm{B}, \mathrm{C}$ in the ABC . Processing times are given Obtain the optimal sequence that minimizes the total elapsed time.

| Job: | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :---: | :--- | :--- | :--- | :---: |
| M1: | 3 | 12 | 5 | 2 | 7 | 11 |
| M2: | 8 | 6 | 4 | 6 | 3 | 1 |
| M3: | 13 | 14 | 9 | 12 | 8 | 13 |

b) Solve the $2 \times 5$ game graphically

## Player B

Player A $\left[\begin{array}{ccccc}-5 & 5 & 0 & -1 & 8 \\ 8 & -4 & -1 & 6 & -5\end{array}\right]$
20. a) A project has the following characteristics
Activity
A B C
D $\quad \mathrm{E} \quad \mathrm{F} \quad \mathrm{G}$
H
I J K

Preceding
Activity : $\quad-\quad-\quad$ A $\quad$ B A B C,D $\quad$ G,F $\quad$ E H,I J
Draw the network diagram.
b) Time estimates for the activities of a PERT network are given

| activity: | $1-2$ | $1-3$ | $1-4$ | $2-5$ | $3-5$ | $4-6$ | $5-6$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{t}_{0}:$ | 1 | 1 | 2 | 1 | 2 | 2 | 3 |  |
| $\mathrm{t}_{\mathrm{m}}:$ | 1 | 4 | 2 | 1 | 5 | 5 | 6 |  |
| $\mathrm{t}_{\mathrm{p}}:$ | 7 | 7 | 8 | 1 | 14 | 8 | 15 |  |

i) Draw the network
ii) Find the expected project length
iii) find variance and Standard deviation for the project length
iv) What is the probability that the project will be completed
a) atleast 4 weeks earlier than expected time?
b) no more than 4 weeks later than expected time?

## hachach

