

M.A. DEGREE EXAMINATION NOVEMBER 2007
BRANCH III – ECONOMICS
FIRST SEMESTER

COURSE : ELECTIVES
PAPER : MATHEMATICAL METHODS - I
TIME : 3 HOURS

MAX.MARKS : 100

SECTION – A

ANSWER ANY FIVE QUESTIONS

(5 X 8 = 40)

1. Explain Continuity of a function at a point giving suitable example.
2. a) Explain the significance of first and second derivatives in economics. Give examples.
b) Examine Convexity of the function

$$y = 2x - 3 + \frac{1}{x}$$

3. Establish the relationship between AR,MR and elasticity of demand given the demand function

$$p = \sqrt{20 - Q}.$$

4. The demand and cost functions of the product produced by a discriminating monopolist are.
 $x_1 = 21 - 0.1P_1$
 $x_2 = 50 - 0.4P_2$
 $C = 10x + 2000.$
Where x_1 & x_2 are the quantities of the product sold by the monopolist in 2 markets. & P_1 & P_2 are the respective prices charged in the market. C – Cost & $x =$ total output, $x = x_1 + x_2$. Determine the prices that the monopolist would charge in the two markets so that Profits are maximized.
5. Explain the properties of Cubb-Douglas Production function.
6. Derive the slope of indifference Curve.
7. Evaluate $\int x^2 e^x dx.$

SECTION – B**ANSWER ANY THREE QUESTIONS****(3 X 20 = 60)**

8. A firm under imperfect competition has the following demand and cost functions:
 $P = 50 - x; C = 20 + 2x + 3x^2$.
- Determine equilibrium Price & quantity which will maximise Profit.
 - If a tax of Rs 5 per unit of product is imposed determine price & quantity that will maximise Profit.
 - If a tax of t per unit of product imposed determine the tax rate which maximises the total tax revenue.
 - If a tax of 20% imposed on sales. determine the equilibrium quantity.
9. Maximise utility Function $u = (x + 2)(y + 1)$ subject to the budget Constraint
 $4x + 6y = 130$.
10.
 - Show that elasticity of substitution of the CES Production Function is constant.
 - Prove Euler's Theorem for CES Production Function.
11. Derive Slutsky's equation.
12. Explain Solow's model.
