SUBJECT CODE: 15MT/ME/NM55

## B. Sc. DEGREE EXAMINATION, APRIL 2019 <br> BRANCH I - MATHEMATICS <br> SIXTH SEMESTER

## COURSE : MAJOR ELECTIVE <br> PAPER : NUMBERICAL METHODS WITH PROGRAMS IN C (THEORY) <br> TIME : 112 HOURS <br> MAX. MARKS: 60

## SECTION-A

## ANSWER ALL QUESTIONS: <br> $$
10 \times 2=20
$$

1. What is the order of convergence of Newton Raphson Method?
2. Give the names of any 2 iteration methods for solving algebraic equations.
3. Find the divided difference table for the following data

| $x$ | 0 | 2 | 3 | 4 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 4 | 26 | 58 | 112 | 466 | 668 |

4. When should we use Newton's backward interpolation formula.
5. Write the formula for computing $\frac{d y}{d x}$ and $\frac{d^{2} y}{d x^{2}}$ at $x=x_{n}$ based on Newton's backward interpolation formula.
6. Write the formula to compute $f^{\prime \prime}\left(x_{k}\right)$ by the method of undetermined coefficients.
7. Write the composite trapezoidal rule.
8. Write Simpson's $3 / 8^{\text {th }}$ rule.
9. Solve $y^{\prime}+y=0, y(0)$ for $x=0.1$ by Euler's method.
10. Write $k_{2}, k_{4}$ values in Runge-kutta's formula of $4^{\text {th }}$ order.

## SECTION-B

## ANSWER ANY FIVE QUESTIONS:

$$
5 \times 8=40
$$

11. Find a real root of the equation $X^{3}-3 x+1=0$ lying between 1 and 2 by using bisection method.
12. Solve the following equation using Jacobi's iteration method

$$
3 x+4 y+15 z=54.8, \quad x+12 y+3 z=39.66, \quad 10 x+y-2 z=7.74
$$

13. The population of a town in the census is as given in the data. Estimate the population in the year 1996 using Newton's forward interpolation formula.

| Year $(x)$ | 1961 | 1971 | 1981 | 1991 | 2001 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Population $(y)$ | 46 | 66 | 81 | 93 | 101 |

14. Use Newton's divided difference formula to find $f(5)$ and $f(9)$ from the following data.

| $X$ | 0 | 2 | 3 | 4 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 4 | 26 | 58 | 112 | 466 | 668 |

15. Find the values of $f^{\prime \prime}(5)$ from the following table, using numerical differentiation based on Newton's backward interpolation formula.

| $x$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 4930 | 5026 | 5122 | 5217 | 5312 | 5407 |

16. Evaluate $\int_{0}^{10} \frac{d x}{1+x^{2}}$ by using
i. Trapezoidal rule.
ii. Simpson $1 / 3^{\text {rd }}$ rule.
17. Given $y^{\prime}=x^{2}-y, y(0)=1$ find $y(0.1)$ using RungeKutta's $4^{\text {th }}$ order.

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## SECTION-C

## ANSWER ANY TWO QUESTIONS:

1. Write a C program to compute the smallest positive root of the equation $f(x)=x^{3}+3 x-1$ by Newton-Raphson method.
2. Write a C program to find $y$, where $x=6$, using the given pairs of values of $x$ and $y$ by Lagrange's's interpolation formula.

| $x$ | 4 | 5 | 7 | 10 | 11 | 13 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 48 | 100 | 294 | 900 | 1210 | 2028 |

3. Write a C program to find the derivative of the tabulated function at the final point by Newton's backward interpolation formula.

| x | 50 | 51 | 52 | 53 | 54 | 55 | 56 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| y | 3.6840 | 3.7084 | 3.7325 | 3.7563 | 3.7798 | 3.8030 | 3.8259 |

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## SECTION-C

ANSWER ANY TWO QUESTIONS:

$$
2 \times 20=40
$$

1. Write a C program to find the smallest positive root / the largest negative root of the equation $f(x)=0$, by using the bisection method.
2. Write a C program to find the derivative at the initial point of a tabulated function by Newton's forward interpolation formula.
3. Write a C program to solve simultaneous differential equations $\frac{d y}{d x}=f(x, y, z)$, $\frac{d z}{d x}=g(x, y, z), y\left(X_{0}\right)=Y_{9}, z\left(X_{0}\right)=Z_{0} \quad$ at the specified pivotal points, by using Runge - Kutta method of the fourth order.
