## SUBJECT CODE : 15MT/AC/MS45

## B. C. A. DEGREE EXAMINATION, APRIL 2019 <br> FOURTH SEMESTER <br> PAPER : MATHEMATICS FOR COMPUTER SCIENCE-II <br> TIME : 3 HOURS MAX. MARKS : 100

COURSE : ALLIED CORE

## SECTION - A

## ANSWER ALL THE QUESTIONS:

1. When you say that two graphs are isomorphic?
2. Define minimal spanning tree.
3. Find the first approximation of the root lying between 0 and 1 of the equation
$x^{3}+3 x-1=0$ by Newton-Raphson formula.
4. State Newton's forward interpolation formula for equal intervals.
5. State stirling's formula.
6. Write the Lagrange's interpolation formula.
7. Evaluate $\int_{0}^{1} e^{-x^{2}} d x$ by dividing the range into 4 equal parts using Trapezoidal rule.
8. Find the first approximation for $\frac{d y}{d x}=1+x y, y(0)=2$ by Picard's method.
9. What is correlation?
10. Mention any two properties of regression coefficients.

## SECTION - B

## ANSWER ANY FIVE QUESTIONS:

11. Prove that a finite connected graph is eulerian if and only if each vertex has even degree.
12. Let $G$ be a connected planar graph with $p$ vertices and $q$ edges, where $p \geq 3$. Then prove that $q \geq 3 p-6$.
13. Solve the following system of equations using Gaussian elimination method
$x+y+z=9 ; 2 x-3 y+4 z=13 ; 3 x+4 y+5 z=40$.
14. Is the system of equations diagonally dominant? If not make it diagonaly dominant. $3 x+9 y-2 z=10 ; 4 x+2 y+13 z=19 ; 4 x-2 y+z=3$.
15. Apply Gauss forward interpolation formula to find $y(25)$ for the following data:

| $x$ | 20 | 24 | 28 | 32 |
| :--- | :--- | :--- | :--- | :--- |
| $y$ | 2854 | 3162 | 3544 | 3992 |

16. For the given data

| $x$ | 0 | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $y(x)$ | 1 | 1 | 15 | 40 | 85 |

find $y^{\prime}(x)$ at $x=0.5$
17. The following are the ranks obtained by 10 students in Statistics and Mathematics:

| Statistics | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Mathematics | 1 | 4 | 2 | 5 | 3 | 9 | 7 | 10 | 6 | 8 |

To what extent is the knowledge of students in the two subjects related?

## SECTION - C

## ANSWER ANY TWO QUESTIONS:

18. (a) Prove that any planar graph is 5 colourable.
(b) Find the positive real root of $x \log _{10} x=1.2$ using bisection method in four iterations.
(10 marks)
19. (a) Find the value of $y$ from the following data at $x=2.65$.

| $X$ | -1 | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ | -21 | 6 | 15 | 12 | 3 |

(b) Evaluate $\int_{0}^{10} \frac{d x}{1+x^{2}}$ by using (i) Trapezoidal rule (ii) Simpson one third rule.
20. Find the equation of regression lines for the following data.

| x | 25 | 28 | 35 | 32 | 36 | 36 | 29 | 38 | 34 | 32 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| y | 43 | 46 | 49 | 41 | 36 | 32 | 31 | 30 | 33 | 39 |

